


Why r^2 is meaningless

Bendix Carstensen Steno Diabetes Center
Gentofte, Denmark
<http://BendixCarstensen.com>

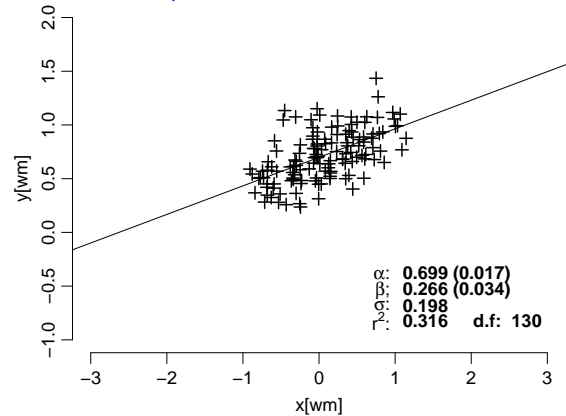
March 2015

<http://BendixCarstensen.com/r-sq.pdf>



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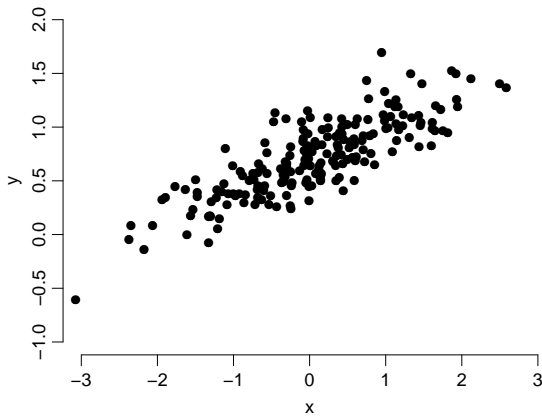
The middle 2/3 of the data



Same estimates of α , β and σ but **smaller** r^2

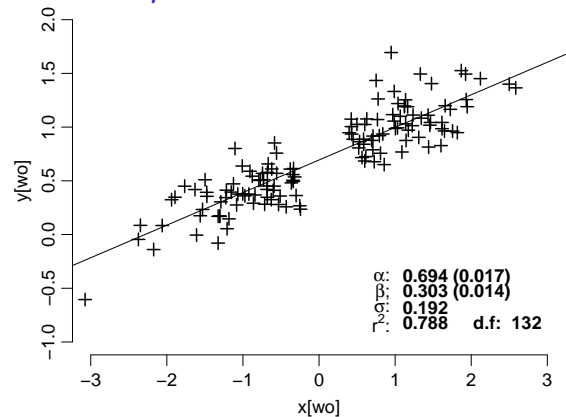
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A dataset



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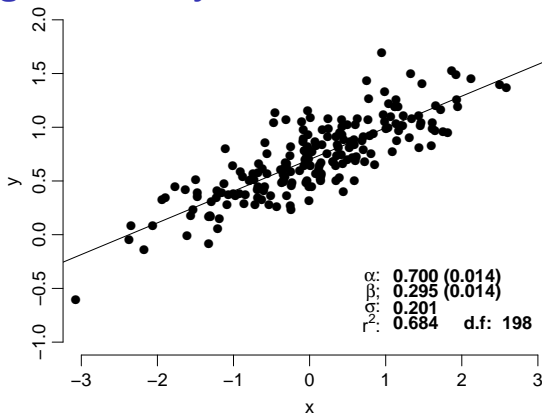
The outer 2/3 of the data



Same estimates of α , β and σ but **larger** r^2

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Regression analysis



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What r^2 is and is not

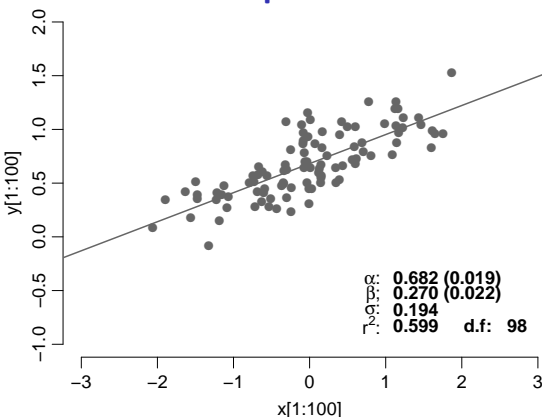
- ▶ r^2 is related to the **population** analysed:
It is the fraction of the **population** variation in y which explained by x .
- ▶ r^2 does **not** convey **any** information on the **size** of the relationship. The relationship is judged from the estimates of α and β :
Is the effect clinically relevant?.
- ▶ r^2 does **not** convey any information on the **precision of predictions**. This is contained in the residual variation, σ . A 95% prediction interval for given $x = x_0$ is:

$$\hat{y}_0 = \hat{\alpha} + \hat{\beta} \times x_0 \pm 1.96\hat{\sigma}$$

(disregarding the estimation error in α and β).

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A 50% random sample



Same estimates of α , β and σ and **same** r^2

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Moral:

- ▶ The clinically relevant parameters α , β and σ are the same no matter how the population is sampled.
- ▶ They reflect the relationship between y and x .
- ▶ r^2 involves the population distribution, which is alien to the relationship between y and x .
- ▶ Hence, r^2 is mathematical mumbo-jumbo where the link to subject matter relevance has been obscured by mixing in the distribution of y in the study population.

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