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Measures of disease frequency and effects

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Key references

IS: dos Santos Silva, I. (1999).
Cancer Epidemiology: Principles and Methods.
International Agency for Research on Cancer,
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B&D: Breslow, N.E., Day, N.E. (1987).

Statistical Methods in Cancer Research Vol. II –
The Design and Analysis of Cohort Studies.
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C&H: Clayton, D., Hills, M. (1993).
Statistical Models in Epidemiology. OUP, Oxford.

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BASIC CONCEPTS

What is epidemiology?

Some textbook definitions:

- "study of the distribution and determinants of disease frequency in man" (MacMahon and Pugh 1970)
- "study of the distribution and determinants of health related states and events in specified populations, ..." (Porta (ed.) Dictionary of Epidemiology, 2008)
- "discipline on principles of occurrence research in medicine" (Miettinen 1985)

Different epidemiologies

- descriptive epidemiology monitoring & surveillance of diseases for planning of health services
 a major activity of cancer registries.
- etiologic or "analytic" epidemiology study of cause-effect relationships
- disease epidemiologies e.g. of cancer, cardiovascular diseases, infectious diseases, musculoskeletal disorders, mental health, . . .
- ▶ **determinant-based** epidemiologies *e.g.* occupational epidemiology, nutritional epidemiology, . . .
- clinical epidemiology study of diagnosis, prognosis and effectiveness of therapies in patient populations
 - basis of evidence-based medicine

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Frequency (from Webster's Dictionary)

 $\label{eq:cowd} \mbox{Etymology:} < \mbox{L } \mbox{\it frequentia} = \mbox{assembly, multitude, crowd.}$

- 2. rate of occurrence
- 3. *Physics.* number of ... regularly occurring events ... in unit of time,
- Statistics. the number of items occurring in a given category. Cf. relative frequency.

Meanings 3. and 5. are both relevant in epidemiology. But what are **rate** and **occurrence**?

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Cancer in Norden 1997 (NORDCAN)

Frequency of cancer (all sites excl. non-melanoma skin) in Nordic male populations expressed by different measures.

| | New cases | Crude rate | ASR (World) | Cumul. risk | SIR |
|---------|--------------|---------------|----------------|----------------|-----------|
| Denmark | 11 787 | 452 | 281 | 27.8 | 104 |
| Finland | 10 058 | <u>401</u> | 269 | 26.5 | 101 |
| Iceland | 633 | 464 | 347 | 32.6 | 132 |
| Norway | 10 246 | 469 | 294 | 29.4 | 109 |
| Sweden | 19 908 | 455 | <u>249</u> | <u>25.4</u> | <u>93</u> |
| | | | | | |

- ▶ Where is the frequency truly **highest**, where <u>lowest</u>?
- ► What do these measures mean?

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Questions on frequency & occurrence

How many women in Denmark

- ▶ are carriers of breast cancer today at 12? prevalence
- ▶ will contract a new breast ca. during 2009? incidence
- ▶ die from breast ca. in 2009? mortality
- will be alive after 5 years since diagnosis among those getting breast ca. in 2009? – survival
- ▶ are cured of breast cancer during 2009? cure

What are the **proportions** or/and **rates** of occurrence of these states and events?

Questions on frequency & occurrence

- ▶ How great are the risks of these events?
- ► Is the frequency/occurrence/risk of breast ca. greater among nulliparous than parous women?
- What are the excess and relative risks for nulliparous compared to parous women?
- What is the dose-response relationship between occupational exposure to crystalline silica and the risk of getting lung cancer in terms of level and length of exposure?

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What is risk?

What do we mean by "risk of disease S"?

- (a) probability of getting S during a given risk period
 → incidence probability,
- (b) rate of change of that probability \rightarrow hazard or intensity,
- (c) **probability** of *carrying* S at a given *time point* \rightarrow **prevalence** probability.

Most commonly meaning (a) is attached with risk.

NB. "Risk" should not be used in the meaning of **risk factor** However, in **risk assessment** literature: "hazard" is often used in that meaning. In statistics, though, hazard refers to notion (b): change of probability per unit time.

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Risks are conditional probabilities

- ► There are no "absolute risks".
- ▶ All risks are conditional on a multitude of factors, like
 - length of risk period (e.g. next week or lifetime),
 - age and gender,
 - genetic constitution,
 - health behaviour & environmental exposures.
- In principle each individual has an own quantitative value for the risk of given disease in any defined risk period, depending on his/her own risk factor profile.
- ▶ Yet, these individual risks are latent and unmeasurable.
- Average risks of disease in large groups sharing common characteristics (like gender, age, smoking status) are estimable from appropriate epidemiologic studies by pertinent measures of occurrence.

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Descriptive and causal studies

- Descriptive: What is the occurrence of lung cancer workers exposed to silica dust as compared to that in subjects of other occupations?
- ► Causal: What is the risk of lung cancer among silica dust workers as compared to ... what the risk in these same men would be, had they not been exposed to silica?

NB. Causal question – **counterfactual conditional**! Challenge: *How to find a* **comparable** *group of unexposed?*

Types of epidemiologic studies

Can crudely be classified in following axes:

- study unit: individual aggregate (ecological study)
- ▶ allocation of exposure: experimental observational
- population: closed (cohort) open (dynamic)
- ► dimensionality: cross-sectional longitudinal
- timing of observations: concurrent historical ("pro-" vs. "retrospective")
- ► sampling of exposure data: cohort case-control

Focus in this course: observational, and longitudinal cohort & case-control studies.

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Experimental and observational studies

Allocation of exposure in etiologic studies?

- **Experimental**: Exposure controlled by investigators, its levels being **randomized** among the study subjects.
 - + Comparability of exposure groups.
 - + Feasible in clinical and preventive trials.
 - Ethically impossible for hazardous exposures.
- **Observational**: Exposure imposed by the own behaviour of the subjects themselves & and by their environment.
 - Possibility of confounding: due to other determinants of the outcome, correlated with exposure.
 - * Challenges: Valid: and efficient non-randomized design and statistical analysis.

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Study population

Types of study population & its membership defined

- ► closed cohort: members taken by certain event, e.g.
 - (i) birth cohort, people born during same year,
 - (ii) workers employed by Carlsberg brewery during 1970's, followed up since then, even after retirement

Once taken in, you can't escape from a cohort.

- ▶ open dynamic: defined by changeable status, e.g.
 - (i) citizens of Copenhagen, currently resident;
 - (ii) catchment population of the Oncological Clinic at Rigshospitalet (CPH),

One may leave an open pop'n and come back to it.

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Study base and its dimensionality

Study base

= Study population \times its experience in time.

Dimensionality of study base

► Cross-sectional:

Study base = study population at a defined time point.

 e.g. all newborn in Denmark 2009 at their dates of birth.

► Longitudinal:

Study base comprises **follow-up times** of individuals in the study population over a given period.

Causal research \rightarrow longitudinal base preferred.

Study base (cont'd)

Longitudinal base:

- (a) Cohort: Individual time intervals from entry until exit, at which the outcome or censoring occurs.
- (b) *Dynamic population:* Each subject contributes possibly several time intervals of membership since the 1st entry until the 'final' exit.
 - ▶ Person-time calculation complicated.
 - Population-based annual (or 5-year period) incidence and mortality statistics:

 $Y \approx \textit{mid-population} \times \text{length of period}.$

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Measurement of exposures and outcomes (IS, ch.2)

In epidemiological studies, it is neccessary to measure

- (1) the primary exposure(s) of interest,
- (2) other exposure(s), potential confounders and modifiers,
- (3) the outcome(s) of interest.

Many approaches, e.g.

- personal interviews & questionnaires, diaries,
- hospital records, other routine data,
- biological and environmental measurements.

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MEASURING FREQUENCY

Quantification of the occurence of disease (or any other health-related state or event) requires specification of:

- (1) what is meant by a **case**, *i.e.*, an individual in a population who has or gets the disease
 - (more generally: possesses the state or undergoes the event of interest).
 - ⇒ challenge to accurate diagnosis and classification!
- (2) the population from which the cases originate.
- (3) the time point or period of observation.

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Types of occurrence measures

- ▶ Longitudinal incidence measures.
- ► Cross-sectional **prevalence** measures.

General form of frequency or occurrence measures

numerator denominator

Numerator: number of cases observed in the population.

Denominator: generally proportional to the size of the population from which the cases emerge.

Numerator and denominator must cover the same population.

Incidence measures

▶ Incidence proportion (Q) over a fixed risk period:

$$Q = \frac{\text{number of incident (new) cases during period}}{\text{size of pop'n at risk at start of the period}}$$

Also called **cumulative incidence** or "risk" (e.g. IS).

NB. "Cumulative incidence" has other meanings, too.

▶ **Indidence rate** (*I*) over a defined observation period:

$$I = \frac{\text{number of incident (new) cases during period}}{\text{sum of follow-up times of pop'n at risk}}$$

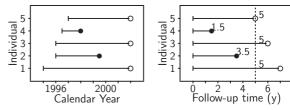
Also called incidence density.

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Example: Follow-up of a small cohort

 \mid = entry, \circ = exit with censoring; outcome not observed,

• = exit with outcome event (disease onset) observed



Complete follow-up in the 5-year risk period

⇒ can calculate both measures:

Inc. rate = $\frac{2 \text{ cases}}{5+3.5+5+1.5+5 \text{ years}} = 10 \text{ per } 100 \text{ years}$ Inc. prop. = $2/5 = 0.4 \ (40 \ \%)$

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Properties of incidence proportion

- ► Dimensionless quantity ranging from 0 to 1 (0% to 100%) = relative frequency,
- ► Estimates the average theoretical risk or probability of the outcome occurring during the risk period, in the population at risk – i.e. among those who are still free from the outcome at the start of the period,
- Simple formula valid when the follow-up time is fixed & equals the risk period, and when there are no competing events or censoring (see below),
- Competing events & censoring ⇒ Calculations need to be corrected using special methods of survival analysis.

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Properties of incidence rate

- ► Like a frequency quantity in physics; measurement unit: e.g. Hz = 1/second, 1/year, or 1/1000 y.
- ► Estimates the average underlying **intensity** or **hazard rate** of the outcome in a population,
- Estimation accurate in the constant hazard model,
- Calculation straightforward also with competing events and censored observations.
- ► Hazard depends on age (& other time variables)
 ⇒ rates specific to age group etc. needed,
- Incidence proportions can be estimated from rates.
 In the constant hazard model with no competing risks:

$$Q = 1 - \exp(-I \times \Delta) \approx I \times \Delta$$

Competing events and censoring

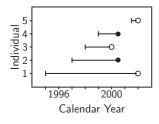
The outcome event of interest (e.g. onset of disease) is not always observed for all subjects during the chosen risk period.

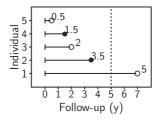
- ▶ Some subjects die (from other causes) before the event.
 - ⇒ Death is a competing event after which the outcome cannot occur any more.
- Others emigrate and escape national disease registration, or the whole study is closed "now", which prematurely interrupts the follow-up of some individuals
 - $\Rightarrow\,$ censoring, withdrawal, or loss to follow-up

Competing events and censorings require special statistical treatment in incidence and risk calculations.

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Follow-up of another small cohort





Two censored observations \Rightarrow can calculate the rate:

$$I = 2/12.5 \text{ y} = 16 \text{ per } 100 \text{ years}$$

but the 5-year $\it Q$ IS NO MORE $\it 2/5$! However, under constant rate model and in the absence of competing risks:

$$Q = 1 - \exp(-5 \times 2/12.5) = 0.55$$

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Person-years in dynamic populations

With dynamic study population individual follow-up times are always variable and impossible to measure accurately.

Common approximation - mid-population principle:

- (1) Let the population size be N_{t-1} at start and N_t at the end of the observation period t with length L_t years,
- (2) Mid-population for the period: $\bar{N}_t = \frac{1}{2} \times (N_{t-1} + N_t)$.
- (3) Approximate person-years: $Y_t \approx \bar{N}_t \times L_t$.

NB. The actual study population often contains also some already affected, who thus do not belong to the population at risk. With rare outcomes the influence of this is small.

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Male person-years in Finland 1991-95

Total male population (1000s) on 31 December by year:

Approximate person-years (1000s):

1992:
$$\frac{1}{2} \times (2443 + 2457) \times 1 = 2450$$

1993-94: $\frac{1}{2} \times (2457 + 2482) \times 2 = 4937$
1991-95: $\frac{1}{2} \times (2431 + 2492) \times 5 = 12307.5$

Incidence proportion, rate, and odds (IS, Ex

4.5)

Individuals initially at risk (disease-free) (n=100) Individual currently at

New cases of disease (D=10)Non-diseased individuals (still at risk)

Time (t)Non-diseased individuals (n-D=90)

Assuming a study period of 1 year with complete follow-up:

Incidence proportion
$$Q=10/100=0.10=10\%$$
 Incidence rate $I=10/95$ y $=10.5$ per 100 y Incidence odds $Q/(1-Q)=10/90=0.11=11$ per 100

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Approximate relations btw measures

With sufficiently

- lacktriangle "short" length Δ of risk period and
- "low" risk (say Q < 10%)

the incidence proportion ${\cal Q}$, rate ${\cal I}$ and odds are approximately related:

$$\frac{Q}{1-Q}\approx Q\approx I\times \Delta$$

The "rare disease assumption".

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Mortality

Cause-specific mortality from disease S is described by mortality rates defined like I but

- ightharpoonup cases are *deaths* from S, and
- ▶ follow-up is extended until death or censoring

Cause-specific **mortality proportions** must be corrected for the incidence of **competing causes of death**

Total mortality:

cases are deaths from any cause.

Mortality depends on the incidence and the **prognosis** or **case fatality** of the disease, *i.e.* the **survival** of those affected by it.

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Mathematical concepts describing risks

Analysis of risks = analysis of times to event or failure times or survival data.

T = **time** to outcome event – random variable, which has a probability distribution with

 $F(t) = P(T \le t) =$ risk function (cumul. distrib. f.) = probability of the outcome to occur before t,

 $S(t) \quad = \quad P(T>t) = 1 - F(t) = \ \, \text{survival} \ \, \text{function of} \ \, T,$

 $=\quad \text{probability of avoiding the event up to given time }t,$

f(t) = F'(t) =**density** function of T, S'(t) = f(t)

$$\lambda(t) \quad = \quad -\frac{S'(t)}{S(t)} = \frac{f(t)}{1-F(t)} \text{ intensity or hazard function},$$

$$\begin{array}{lcl} \Lambda(t) & = & \int_0^t \lambda(u) du = -\log S(t) = \text{cumulative hazard}, \\ \Leftrightarrow & F(t) = 1 - \exp\{-\Lambda(t)\}, \quad f(t) = \lambda(t) S(t). \end{array}$$

Hazard and risk

Hazard or intensity can be viewed as **theoretical incidence rate**. Formally defined

$$\lambda(t) = \lim_{\Delta \to 0} \frac{P(t < T \le t + \Delta \mid T > t)}{\Delta}$$

pprox Probability of outcome event occurring in a short risk period $]t,t+\Delta]$, given "survival" or avoidance of the event up to the start t, divided by the period length.

This is equivalent to saying that over a short interval

 $risk \approx intensity \times length of interval$

or
$$P(t < T \le t + \Delta \mid T > t) \approx \lambda(t) \times \Delta$$
.

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Exponential or constant hazard model

Simplest probability model for time to event:

Exponential distribution, $Exp(\lambda)$, in which

rate at any time t: $\lambda(t)=\lambda$, constant over time \Rightarrow risk over period]0,t]: $F(t)=1-\exp(-\lambda t)$

Analysis of event data of n individuals. For subject i let

 $y_i = \text{time to event or censoring, total: } Y = \sum y_i$

 $d_i = 1$ /0-indicator for observing event, total: $D = \sum d_i$

 $\operatorname{Exp}(\lambda) \operatorname{model} \Rightarrow \operatorname{Likelihood} \operatorname{function} \operatorname{of} \lambda \operatorname{is} \operatorname{equivalent} \operatorname{to} \operatorname{that} \operatorname{when} \operatorname{number} \operatorname{of} \operatorname{cases} D \operatorname{would} \operatorname{be} \operatorname{Poisson-distributed}$

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Basic statistical analysis of rates

Asymptotic statistical inference based on likelihood:

▶ Maximum likelihood estimator (MLE) of λ is

$$\widehat{\lambda} = \frac{D}{Y} = \frac{\text{number of cases}}{\text{total person-time}} = I, \text{ empirical incidence rate!}$$

- ▶ **Standard error** of the empirical rate is $I \times 1/\sqrt{D}$
- ⇒ The more cases, the greater is **precision** in rate!
- Approximate **confidence interval** for "true" rate λ :

estimator $\pm~1.96 \times {\rm standard~error}$

More about these issues in Bendix's lectures next week.

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Prevalence measures

Point prevalence or simply **prevalence** P of a health state C in a population at a given time point t is defined

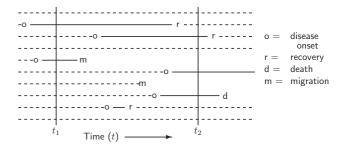
 $P = \frac{\text{number of existing or prevalent cases of } C}{\text{size of the whole population}}$

This is calculable from a cross-sectional study base.

Period prevalence for period from t_1 to t_2 is like P but

- numerator refers to all cases prevalent already at t1 plus new cases occurring during the period, and
- denominator is the population size at t_2 .

Example 4.1 (IS: p. 59)



 $\begin{array}{ll} \mbox{Prevalence at time $t_1:$} & 2/10 = 0.2 = 20\% \\ \mbox{Prevalence at time $t_2:$} & 3/8 = 0.38 = 38\% \\ \mbox{Period prevalence:} & 5/8 = 0.62 = 62\% \end{array}$

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Prevalence and incidence are related

Point prevalence of S at given time point t depends on

- ightharpoonup incidence of new cases of S before t
- duration of S, depending in turn on the probability of cure or recovery from S or survival of those affected

in complicated ways.

Simple special case: In a **stationary** population prevalence (P), incidence (I), and average duration (\bar{d}) of S are related:

$$P = \frac{I \times \bar{d}}{I \times \bar{d} + 1} \approx I \times \bar{d}$$

The approximation works well, when P < 0.1 (10%).

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Prevalence of cancer?

Difficult to ascertain, whether and when a cancer is cured.

⇒ Existing or prevalent cancer case problematic to define.

Cancer registry practice: Prevalence of cancer ${\cal C}$ at time point t in the target population refers to the

number & proportion of population members who

- \triangleright are alive and resident in the population at t, and
- \blacktriangleright have a record of incident cancer C diagnosed before t.

Often further classified by years since diagnosis.

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Example: Liver and testis cancer

Crude comparison of incidence, mortality and prevalence in the male population of Finland 1999

| | Liver | Testis |
|--|-------|--------|
| | | |
| No. of new cases during 1999 | 119 | 103 |
| No. of deaths during 1999 | 123 | 8 |
| No. of prevalent cases 1.1.2000 | 120 | 1337 |
| - " $-$ diagnosed < 1 y ago | 36 | 97 |
| − " − diagnosed 1-< 5 y ago | 53 | 291 |
| − " − diagnosed 5-< 10 y ago | 17 | 304 |
| - " $-$ diagnosed $>$ 10 y ago | 14 | 642 |

COMPARISON OF FREQUENCIES

Quantification of the **association** between a determinant (risk factor or exposure) and an outcome (disease) is based on

comparison of occurrence between the *index* ("exposed") and the *reference* ("unexposed") groups or populations by

- ► relative measures (ratio)
- absolute measures (difference)

In causal studies these are used to estimate the causal effect of the exposure factor on the disease risk.

 \Rightarrow comparative measures \approx effect measures

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Relative comparative measures

Generic name **"relative risk"** RR comparing occurrences between exposed (1) and unexposed (0) groups can refer to

- incidence rate ratio I_1/I_0 ,
- incidence proportion ratio Q_1/Q_0 ,
- incidence odds ratio $[Q_1/(1-Q_1)]/[Q_0/(1-Q_0)]$,
- ▶ prevalence ratio P_1/P_0 , or
- prevalence odds ratio $[P_1/(1-P_1)]/[P_0/(1-P_0)]$,

depending on study base and details of its design.

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Absolute comparative measures

Generic "excess risk" or "risk difference" (RD) btw exposed and unexposed can refer to

- incidence rate difference $I_1 I_0$,
- ightharpoonup incidence proportion difference Q_1-Q_0 , or
- ▶ prevalence difference $P_1 P_0$.

Use of relative and absolute comparisons

- Ratios describe the biological strength of the exposure
- Differences inform about its public health importance.

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Example: (IS, Table 5.2, p.97)

Relative and absolute comparisons between the exposed and the unexposed to risk factor \boldsymbol{X} in two diseases.

| | Disease A | Disease B |
|---|-----------|-----------|
| Incidence rate among exposed ^a | 20 | 80 |
| Incidence rate among unexposed ^a | 5 | 40 |
| Rate ratio | 4.0 | 2.0 |
| Rate difference ^a | 15 | 40 |

^a Rates per 100 000 pyrs.

Factor X has a stronger biological potency for disease A, but it has a greater public health importance for disease B.

Ratio measures in "rare diseases"

(IS: Ex 5.13)

| | Exposure | | |
|-----------------------|----------|--------|--|
| _ | Yes | No | |
| No. initially at risk | 4 000 | 16 000 | |
| Deaths | 30 | 60 | |
| Person-years at risk | 7 970 | 31 940 | |

Inc. prop'n ratio =
$$\frac{30/4\,000}{60/16\,000}$$
 = $\frac{7.5\,\mathrm{per}\,1\,000}{3.75\,\mathrm{per}\,1\,000}$ = 2.0000
Inc. rate ratio = $\frac{30/7\,970\,\mathrm{y}}{60/31\,940\,\mathrm{y}}$ = $\frac{3.76\,\mathrm{per}\,1\,000\,\mathrm{y}}{1.88\,\mathrm{per}\,1\,000\,\mathrm{y}}$ = 2.0038
Inc. odds ratio = $\frac{30/(4\,000-30)}{60/(16\,000-60)}$ = $\frac{0.00756}{0.00376}$ = 2.0076

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Measures of potential impact

Combine absolute and relative comparisons.

When incidence is higher for the exposed, we can calculate

Excess fraction, EF
$$= \frac{Q_1 - Q_0}{Q_1} = \frac{\mathsf{RR} - 1}{\mathsf{RR}}$$

also called attributable fraction (or "attributable risk").

EF estimates the fraction out of all new cases among those exposed, which are "caused" by the exposure itself, and which thus could be "avoided" if the exposure were absent

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Next time: Graphics of impact measures

Apply Bendix's R script on how to draw pictures to illustrate the concepts of excess fraction and population excess fraction with given RRs and prevalences of exposure.

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Measures of potential impact (cont'd)

When the exposed have a lower incidence, we can calculate

Prevented fraction,
$$PF = \frac{Q_0 - Q_1}{Q_0} = 1 - RR$$

also called **relative risk reduction** = percentage of cases prevented among the exposed due to the exposure.

Used to evaluate the relative effect of a preventive intervention (exposed) vs. no intervention (unexposed).

Population EF and **population PF** combine these further with the *prevalence of exposure* in target population.

Effect of smoking on mortality by cause

(IS: Example 5.14, p. 98)

| Underlying cause of death | Never smoked regularly Rate ^b | Current cigarette smoker Rate ^b | Rate ratio | Rate differ- ence ^b | Excess fraction (%) |
|---------------------------------|---|---|---------------|--------------------------------------|----------------------------------|
| | (1) | (2) | (2)/(1) | (2) - (1) | $\frac{(2)-(1)}{(2)} \times 100$ |
| Cancer | | | | | |
| All sites | 305 | 656 | 2.2 | 351 | 54 |
| Lung | 14 | 209 | 14.9 | 195 | 93 |
| Oesophagus | 4 | 30 | 7.5 | 26 | 87 |
| Bladder Respiratory diseases | 13 | 30 | 2.3 | 17 | 57 |
| (except cancer) | 107 | 313 | 2.9 | 206 | 66 |
| Vascular diseases | 1037 | 1643 | 1.6 | 606 | 37 |
| All causes | 1706 | 3038 | 1.8 | 1332 | 44 |

a Data from Doll et al., 1994a

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RATES BY VARIOUS TIME AXES

Incidence can be studied on various time scales, e.g.

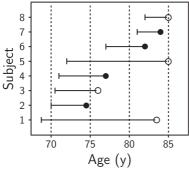
- ▶ age (starting point = birth),
- exposure time (first exposure),
- ▶ follow-up time (entry to study),
- duration of disease (diagnosis).

Age is usully the strongest time-dependent determinant of health outcomes.

Age is also often correlated with duration of "chronic" exposure (e.g. years of smoking).

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Follow-up of a small geriatric cohort



Overall rate: 4 cases/53.5 person-years = 7.5 per 100 y Hides the fact that the "true" rate probably varies by age, being higher among the old.

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Splitting follow-up into agebands

- To describe, how incidence varies by age, individual person-years from age of entry to age of exit must first be split or divided into narrower agebands.
- ▶ Usually these are based on common 5-year age grouping.
- ▶ Numbers of cases are equally divided into same agebands.
- ightharpoonup Age-specific incidence rate for age group k is
 - $I_k = \frac{ ext{number of cases observed in ageband}}{ ext{person-years contained in ageband}}$
- Underlying assumption: piecewise constant rates model

Person-years and cases in agebands: age-specific rates

| | | Ageband | | | | |
|---------------------|-------|---------|-------|-------|--|--|
| Subject | 70-74 | 75-79 | 80-84 | Total | | |
| 1 | 5.0 | 5.0 | 3.5 | 13.5 | | |
| 2 | 4.5 | - | - | 4.5 | | |
| 3 | 4.5 | 1.0 | - | 5.5 | | |
| 4 | 4.0 | 2.0 | _ | 6.0 | | |
| 5 | 3.0 | 5.0 | 5.0 | 13.0 | | |
| 6 | - | 3.0 | 2.0 | 5.0 | | |
| 7 | - | - | 3.0 | 3.0 | | |
| 8 | - | - | 3.0 | 3.0 | | |
| Sum of person-years | 21.0 | 16.0 | 16.5 | 53.5 | | |
| Cases | 1 | 1 | 2 | 4 | | |
| Rate (/100 y) | 4.8 | 6.2 | 12.1 | 7.5 | | |
| | Age- | overall | | | | |
| | | | | | | |

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Ex. Lung cancer incidence in Finland by age and period (compare IS, Table 4.1)

| Calendar | Age group (y) | | | | | | | | | |
|----------|---------------|-------|-------|-------|-------|-------|-------|-------|-------|-----|
| period | 40-44 | 45-49 | 50-54 | 55-59 | 60-64 | 65-69 | 70-74 | 75-79 | 80-84 | 85+ |
| 1953-57 | 21 | 61 | 119 | 209 | 276 | 340 | 295 | 279 | 193 | 93 |
| 1958-62 | 22 | 65 | 135 | 243 | 360 | 405 | 429 | 368 | 265 | 224 |
| 1963-67 | 24 | 61 | 143 | 258 | 395 | 487 | 509 | 479 | 430 | 280 |
| 1968-72 | 21 | 61 | 134 | 278 | 424 | 529 | 614 | 563 | 471 | 358 |
| 1973-77 | 16 | 50 | 134 | 251 | 413 | 541 | 629 | 580 | 490 | 392 |
| 1978-82 | 13 | 36 | 115 | 234 | 369 | 514 | 621 | 653 | 593 | 442 |
| 1983-87 | 11 | 31 | 74 | 186 | 347 | 450 | 566 | 635 | 592 | 447 |
| 1988-92 | 9 | 25 | 57 | 128 | 262 | 411 | 506 | 507 | 471 | 441 |
| 1993-97 | 7 | 22 | 48 | 106 | 188 | 329 | 467 | 533 | 487 | 367 |
| 1998-02 | 5 | 14 | 46 | 77 | 150 | 239 | 358 | 445 | 396 | 346 |

- ▶ Rows: age-incidence pattern in different calendar periods.
- ► Columns: Trends of age-specific rates over calendar time.

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Lung cancer rates by age and period

- Age-incidence curves: overall level and peak age variable across periods.
- ▶ Time trends inconsistent across age groups.

54/ 9

Incidence by age, period & cohort

 Secular trends of specific and adjusted rates show, how the "cancer burden" has developed over periods of calendar time.

Birth cohort = people born during the same limited time interval, e.g. single calendar year, or 5 years period.

- Analysis of rates by birth cohort reveals, how the level of incidence (or mortality) differs between successive generations – may reflect differences in risk factor levels.
- Often more informative about "true" age-incidence pattern than age-specific incidences of single calendar period.

b Age-adjusted rates per 100 000 pyrs.

Age-specific rates by birth cohort

| Calendar | Age group (y) | | | | | | | | |
|----------|---------------|-------|-------|-------|-------|-------|-------|-------|---|
| period | 40-44 | 45-49 | 50-54 | 55-59 | 60-64 | 65-69 | 70-74 | 75-79 | |
| 1953-57 | 21 | 61 | 119 | 209 | 276 | 340 | 295 | 279 | |
| 1958-62 | 22 | 65 | 135 | 243 | 360 | 405 | 429 | 368 | |
| 1963-67 | 24 | 61 | 143 | 258 | 395 | 487 | 509 | 479 | Α |
| 1968-72 | 21 | 61 | 134 | 278 | 424 | 529 | 614 | 563 | |
| 1973-77 | 16 | 50 | 134 | 251 | 413 | 541 | 629 | 580 | |
| 1978-82 | 13 | 36 | 115 | 234 | 369 | 514 | 621 | 653 | В |
| 1983-87 | 11 | 31 | 74 | 186 | 347 | 450 | 566 | 635 | |
| 1988-92 | 9 | 25 | 57 | 128 | 262 | 411 | 506 | 507 | |
| 1993-97 | 7 | 22 | 48 | 106 | 188 | 329 | 467 | 533 | C |
| 1998-02 | 5 | 14 | 46 | 77 | 150 | 239 | 358 | 445 | |
| | E: 1947/48 | | | | | D: 19 | 32/33 | | |

 $\mathsf{A} = \mathsf{synthetic} \ \mathsf{cohort} \ \mathsf{born} \ \mathsf{around} \ 1887/88, \ \ \mathsf{B:} \ 1902/03, \ \ \mathsf{C:} \ 1917/18$

Diagonals reflect age-incidence pattern in birth cohorts.

56/ 95

Age-incidence curves in 5 birth cohorts

Variable overall levels but fairly consistent form and similar peak age across different birth cohorts.

57/ 95

Split of follow-up by age and period

Incidence of (or mortality from) disease C in special study cohort (e.g. occupational group, users of certain medicine)

→ often compared to incidence in a reference or "general" population

For examples, see Laufey's lecture on cohort studies (*e.g.* atomic bomb survivors, rubber workers, and those exposed to dyestaff)

Adjustment for age and calendar time needed, e.g. by comparing observed to expected cases with SIR (see p. 76-79).

⇒ Cases and person-years in the study cohort must be split by more than one time scale (age).

58/95

Example (C&H, Tables 6.2 & 6.3, p. 54)

Entry and exit dates for a small cohort of four subjects

| Subject | Born | Entry | Exit | Age at entry | Outcome |
|---------|------|-------|------|--------------|-----------------|
| 1 | 1904 | 1943 | 1952 | 39 | Migrated |
| 2 | 1924 | 1948 | 1955 | 24 | Disease C |
| 3 | 1914 | 1945 | 1961 | 31 | Study ends |
| 4 | 1920 | 1948 | 1956 | 28 | Unrelated death |

Subject 1: Follow-up time spent in each ageband

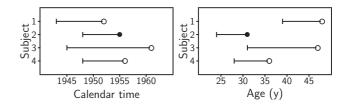
| Age band | Date in | Date out | Time (years) |
|----------|---------|----------|--------------|
| 35-39 | 1943 | 1944 | 1 |
| 40-44 | 1944 | 1949 | 5 |
| 45-49 | 1949 | 1952 | 3 |

Example: (C&H, Figures 6.1 & 6.2, p. 55)

Follow-up of cohort members by calendar time and age

entry

- exit because of disease onset (outcome of interest)
- o exit due to other reason (censoring)

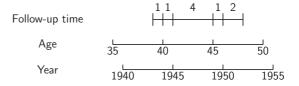


60/95

Person-years by age and period

(C&H, Figure 6.4)

Subject 1: Follow-up jointly split by age and calendar time:

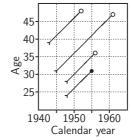


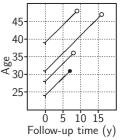
This subject contributes person-time into 5 different cells defined by ageband & calendar period

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Follow-up in Lexis-diagrams

(C&H, pp. 58-59)





Follow-up lines run diagonally through different ages and calendar periods.

See also Laufey's lecture on cohort studies, slide 4.

62/ 9

STANDARDIZATION OF RATES

- ► Incidence of most cancers (and many other diseases) increases strongly by age in all populations.
 - ⇒ Most of the caseload comes from older age groups.
- ► Crude incidence rate is a rate in which:
 - $\,\blacktriangleright\,$ numerator = sum of age-specific numbers of cases,
 - $\begin{tabular}{ll} \bullet & denominator = sum of age-specific person-years. \end{tabular}$
- ► This is generally a poor summary measure.
- ► Comparisons of crude incidences between populations can be very misleading, when the age structures differ.
- ▶ Adjustment or standardization for age needed!

59 / 91

Ex. Male stomach cancer in Cali and Birmingham (IS, Table 4.2, p. 71)

| | | Cali | | | Birmingham | | | |
|-------|-------|-------------------|--------------|-------|------------------|--------------|-------|--|
| | | Male | Incid. | | Male | Incid. | | |
| | Male | Popu- | Rate | Male | Popu- | Rate | | |
| | cases | lation | $(/10^{5}y)$ | cases | lation | $(/10^{5}y)$ | | |
| Age | 1982 | 1984 | 1982 | 1983 | 1985 | 1983 | Rate | |
| (y) | -86 | $(\times 10^{3})$ | -86 | -86 | $(\times 10^3))$ | -86 | ratio | |
| 0-44 | 39 | 524.2 | 1.5 | 79 | 1 683.6 | 1.2 | 1.25 | |
| 45-64 | 266 | 76.3 | 69.7 | 1037 | 581.5 | 44.6 | 1.56 | |
| 65+ | 315 | 22.4 | 281.3 | 2352 | 291.1 | 202.0 | 1.39 | |
| Total | 620 | 622.9 | 19.9 | 3468 | 2 556.2 | 33.9 | 0.59 | |

- ▶ In each age group Cali has a higher incidence but the crude incidence is higher in Birmingham.
- ► Is there a paradox?

64/95

Comparison of age structures (IS, Tables 4.3,4.4)

| | % of male population | | | | | | | |
|----------|----------------------|-------|---------|--------|--|--|--|--|
| Age | Cali | B'ham | Finland | World | | | | |
| (years) | 1984 | 1985 | 1999 | Stand. | | | | |
| 0-44 | 84 | 66 | 61 | 74 | | | | |
| 45-64 | 12 | 23 | 27 | 19 | | | | |
| 65+ | 4 | 11 | 12 | 7 | | | | |
| All ages | 100 | 100 | 100 | 100 | | | | |

The fraction of old men greater in Birmingham than in Cali.

- ⇒ Crude rates are **confounded** by age.
- ⇒ Any summary rate must be **adjusted for age**.

65/ 95

Age-adjustment by standardisation

Age-standardised incidence rate (ASR):

$$\mathsf{ASR} = \sum_{k=1}^K \mathsf{weight}_k \times \mathsf{rate}_k \ / \ \mathsf{sum \ of \ weights}$$

- = Weighted average of age-specific rates over the age-groups $k=1,\ldots,K.$
- ► Weights describe age distribution of some standard population.
- Standard population can be real (e.g. one of the populations under comparison, or their average) or fictitious (e.g. World Standard Population, WSP)

66/95

Some standard populations:

| Age group (years) | African | World | European | Truncated |
|-------------------|---------|---------|----------|-----------|
| 0 | 2 000 | 2 400 | 1 600 | _ |
| 1-4 | 8 000 | 9 600 | 6 400 | _ |
| 5-9 | 10 000 | 10 000 | 7 000 | _ |
| 10-14 | 10 000 | 9 000 | 7 000 | _ |
| 15-19 | 10 000 | 9 000 | 7 000 | _ |
| 20-24 | 10 000 | 8 000 | 7 000 | _ |
| 25-29 | 10 000 | 8 000 | 7 000 | _ |
| 30-34 | 10 000 | 6 000 | 7 000 | _ |
| 35-39 | 10 000 | 6 000 | 7 000 | 6 000 |
| 40-44 | 5 000 | 6 000 | 7 000 | 6 000 |
| 45-49 | 5 000 | 6 000 | 7 000 | 6 000 |
| 50-54 | 3 000 | 5 000 | 7 000 | 5 000 |
| 55-59 | 2 000 | 4 000 | 6 000 | 4 000 |
| 60-64 | 2 000 | 4 000 | 5 000 | 4 000 |
| 65-69 | 1 000 | 3 000 | 4 000 | - |
| 70-74 | 1 000 | 2 000 | 3 000 | - |
| 75-79 | 500 | 1 000 | 2 000 | _ |
| 80-84 | 300 | 500 | 1 000 | - |
| 85+ | 200 | 500 | 1 000 | - |
| Total | 100 000 | 100 000 | 100 000 | 31 000 |

Stomach cancer in Cali & B'ham

Age-standardized rates by the World Standard Population:

| | | Cali | В | irmingham |
|---------|-----------|--------------|----------|--------------|
| Age | $Rate^a$ | Weight | $Rate^a$ | Weight |
| 0-44 | 1.5 × | 0.74 = 1.11 | 1.2× | 0.74 = 0.89 |
| 45-64 | 69.7 × | 0.19 = 13.24 | 44.6 × | 0.19 = 8.47 |
| 65+ | 281.3 × | 0.07 = 19.69 | 202.0 × | 0.07 = 14.14 |
| Ago sta | ndardicad | rato 24.04 | | 22.50 |

- ▶ ASR in Cali higher coherent with the age-specific rates.
- ► Summary rate ratio estimate: standardized rate ratio

$$SRR = 34.0/23.5 = 1.44$$

► Known as **comparative mortality figure (CMF)** when the outcome is death (from cause *C* or all causes).

68/95

Cumulative rate and "cumulative risk"

- ► Choice of standard somewhat arbitrary.
- Alternative and maybe more natural method for age-adjustment is provided by cumulative rate:

$$\mathsf{CR} = \sum_{k=1}^K \mathsf{width}_k \times \mathsf{rate}_k,$$

- ▶ Weights are widths of the agebands to be included.
- ▶ Usually computed up to 65 or 75 y with 5-y bands.
- Often interpreted as approximating the average "cumulative risk" (incidence proportion) to get the disease by 65 or 75 years, given survival until then.
- ▶ Based on relation btw risk F(t) and hazard $\lambda(t)$, or

Inc. prop'n =
$$1 - \exp(-\text{cum. rate}) \approx \text{cum. rate}$$

69/ 95

Stomach cancer in Cali & B'ham

From age-specific rates of Table 4.2. the cumulative rates up to 65 years and their ratio are

Cali:
$$45\ y \times \frac{1.5}{10^5 y} + 20\ y \times \frac{69.7}{10^5 y} = 0.0146 = \textbf{1.46}$$
 per 100 B'ham: $45\ y \times \frac{1.2}{10^5 y} + 20\ y \times \frac{44.6}{10^5 y} = 0.0095 = \textbf{0.95}$ per 100 ratio: $1.46/0.95 = \textbf{1.54}$

Cumulative "risks" & their ratio up to 65 y:

Cali:
$$1 - \exp(-0.0146) = 0.0145 = \mathbf{1.45\%}$$

B'ham: $1 - \exp(-0.0095) = 0.0094 = \mathbf{0.94\%}$
ratio: $1.45/0.94 = \mathbf{1.54}$

NB. For more appropriate estimates of cumulative risks, correction for total mortality (competing event) needed.

70/ 9

Cumulative measures using 5-y groups

(IS, Fig 4.11, p. 77)

| Age-group (years) | Incidence rate (per 100 000 pyrs) |
|-------------------|--------------------------------------|
| 0-4,, 15-19 | 0.0 |
| 20-24, 25-29 | 0.1 |
| 30-34 | 0.9 |
| 35–39 | 3.5 |
| 40-44 | 6.7 |
| 45-49 | 14.5 |
| 50-54 | 26.8 |
| 55–59 | 52.6 |
| 60-64 | 87.2 |
| 65–69 | 141.7 |
| 70–74 | 190.8 |
| Sum | 524.9 |

Cum. rate 0-75 y =
$$5 \text{ y} \times \frac{524.9}{10^5 \text{ y}} = 0.0262 = \textbf{2.6} \text{ per } 100$$
 Cum. "risk" 0-75 y = $1 - \exp(-0.0262) = 0.0259 = \textbf{2.6}\%$.

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Cumulative and life-time risks

Interesting and relevant question

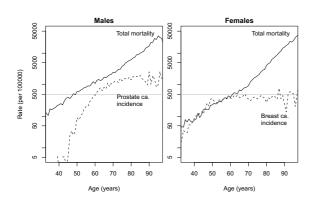
"What are my chances of getting cancer C in the next 10 years, between ages 50 to 75 years, or during the whole lifetime?"

Difficult to answer.

- ► Fully individualized risks are unidentifiable.
- Age-specific and standardized rates are not very informative as such.
- Average cumulative risks are often estimated from cumulative rates
- Yet, these estimates fictitiously presume that a person would not die from any cause before cancer hits him/her, but could even survive forever!

72/ 95

Total mortality and incidence of two common cancers by age, Finland 2005



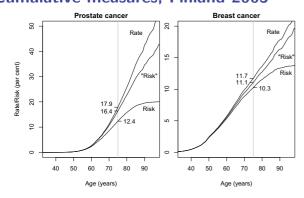
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Estimation of cumulative risks

- ► The probability of contracting cancer during realistic lifespan or in any age range depends not only on age-specific hazard rates of cancer itself but also of probabilities of overall survival up to relevant ages,
- Hence, the dependence of total mortality by age in the population at risk must be incorporated in estimation of cumulative risks of cancer.
- When this is properly done, the corrected estimates of cumulative risk will always be lower than the uncorrected "risks".
- ► The magnitude of bias in the latter grows by age, but is reduced with increased life expectancy.

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Cumulative measures, Finland 2005



Greater differences in males reflect shorter life expectancy and relatively high rates of prostate ca. in old ages.

Special cohorts of exposed subjects

- Occupational cohorts, exposed to potentially hazardous agents (e.g. rubber workers, see Laufey's lecture on cohort studies, slides 19-20)
- ► Cohorts of patients on chronic medication, which may have harmful long-term side-effects
- ▶ No internal comparison group of unexposed subjects.

Question: Do incidence or mortality rates in the exposed target cohort differ from those of a roughly comparable reference population?

Reference rates obtained from:

- population statistics (mortality rates)
- ▶ disease & hospital discharge registers (incidence)

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Observed and expected cases - SIR

- Compare rates in a study cohort with a standard set of age-specific rates from the reference population.
- Reference rates normally based on large numbers of cases, so they are assumed to be "known" without error.
- Calculate expected number of cases, E, if the standard age-specific rates had applied in our study cohort.
- ► Compare this with the **observed** number of cases, *D*, by the **standardized incidence ratio** SIR (or st'zed mortality ratio SMR with death as outcome)

$$SIR = D/E$$
, $SE(log[SIR]) = 1/\sqrt{D}$

77/ 95

Example: HT and breast ca.

- ► A cohort of 974 women treated with hormone (replacement) therapy were followed up.
- ightharpoonup D = 15 incident cases of breast cancer were observed.
- ▶ Person-years (Y) and reference rates $(\lambda_a^*$, per 100000 y) by age group (a) were:

| Age | Y | λ_a^* | E |
|--------|------|---------------|-------|
| 40-44 | 975 | 113 | 1.10 |
| 45-49 | 1079 | 162 | 1.75 |
| 50-54 | 2161 | 151 | 3.26 |
| 55-59 | 2793 | 183 | 5.11 |
| 60-64 | 3096 | 179 | 5.54 |
| \sum | | | 16.77 |

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Ex: HT and breast ca. (cont'd)

► "Expected" cases at ages 40–44:

$$975 \times \frac{113}{100\,000} = 1.10$$

- ▶ Total "expected" cases is E = 16.77
- ightharpoonup SIR = 15/16.77 = 0.89.
- ► Error-factor: $\exp(1.96 \times \sqrt{1/15}) = 1.66$
- ▶ 95% confidence interval is:

$$0.89 \stackrel{\times}{\div} 1.66 = (0.54, 1.48)$$

SIR for Cali with B'ham as reference

Total person-years at risk and expected number of cases in Cali 1982-86 based on age-specific rates in Birmingham (**IS**: Fig. 4.9, p. 74)

| Age | Person-years | Expected cases in Cali |
|-------|----------------------|-----------------------------------|
| 0-44 | 524 220×5= 2 621 100 | 0.000012×2 621 100= 31.45 |
| 45-64 | 76 304×5= 381 520 | $0.000446 \times 381520 = 170.15$ |
| 65+ | 22 398×5= 111 990 | $0.002020 \times 111990 = 226.00$ |

All ages

=3 114 610

Total expected (E) 427.82

Total observed number O=620.

Standardised incidence ratio:

$$\mathsf{SIR} = \frac{O}{E} = \frac{620}{427.8} = 1.45 \quad \text{(or } 145 \ \mathrm{per} \ 100)$$

80/95

Crude and adjusted rates compared

(IS: Table 4.6, p. 78, extended)

| | Cali, 1982-86 | B'ham, 1983-86 | Rate ratio |
|---|------------------|-------------------|---------------|
| Crude rates $(/10^5 \text{ y})$ | 19.9 | 33.9 | 0.59 |
| ASR $(/10^5 \text{ y})^B$ with 3 broad age groups | 48.0 | 33.9 | 1.42 |
| ASR $(/10^5 \text{ y})^C$ –"– | 19.9 | 14.4 | 1.38 |
| ASR $(/10^5 \text{ y})^W$ –"– | 34.0 | 23.5 | 1.44 |
| Cum. rate < 65 y (per 1000) -"- | 14.6 | 9.5 | 1.54 |
| ASR $(/10^5 \text{ y})^W$ with 18 5-year age groups | 36.3 | 21.2 | 1.71 |
| Cum. rate < 75 y (per 1000) -"- | 46.0 | 26.0 | 1.77 |

Standard population: B Birmingham 1985, C Cali 1985, W World SP

NB: The ratios of age-adjusted rates appear less dependent on the choice of standard weights than on the coarseness of age grouping. 5-year age groups are preferred.

81/95

SURVIVAL ANALYSIS OF CANCER

Prognosis of cancer:

▶ what are the patients' chances to **survive** 1 year, 5 years, etc. since diagnosis?

Survival analysis: In principle like incidence analysis but

- population at risk = patients with cancer,
- ▶ basic time variable = time since the date of diagnosis, at which the follow-up starts,
- outcome event of interest = death,
- measures and methods used somewhat different from those used in incidence analysis.

Follow-up of 8 out of 40 breast cancer patients (from IS, table 12.1., p. 264)

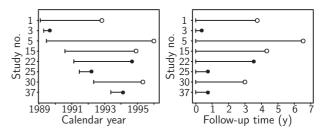
| No. | Age (y) | Sta- ge ^a | Date of diag- nosis | Date at end of follow -up | Vital status at end of follow -up | Cause of death ^c | Full years from diagn's up to end of follow -up | Days from diagn's up to end of follow -up |
|-----|------------|-------------------------|---------------------------|---------------------------------------|--|-----------------------------------|---|---|
| 1 | 39 | 1 | 01/02/89 | 23/10/92 | А | _ | 3 | 1360 |
| 3 | 56 | 2 | 16/04/89 | 05/09/89 | D | BC | 0 | 142 |
| 5 | 62 | 2 | 12/06/89 | 28/12/95 | Α | _ | 6 | 2390 |
| 15 | 60 | 2 | 03/08/90 | 27/11/94 | Α | _ | 4 | 1577 |
| 22 | 64 | 2 | 17/02/91 | 06/09/94 | D | 0 | 3 | 1297 |
| 25 | 42 | 2 | 20/06/91 | 15/03/92 | D | BC | 0 | 269 |
| 30 | 77 | 1 | 05/05/92 | 10/05/95 | Α | - | 3 | 1100 |
| 37 | 45 | 1 | 11/05/93 | 07/02/94 | D | BC | 0 | 272 |

a 1 = absence of regional lymph node involment and metastases

2 = involvment of regional lymph node and/or presence of metastases b A = alive; D = dead; c BC = breast cancer; O = other causes

Follow-up of breast ca. pts (cont'd)

| entry = diagnosis; • exit = death; ∘ exit = censoring



(IS: Figure 12.1, p. 265)

84/95

Life table or "actuarial" method

- (1) Divide the follow-up time into subintervals k = 1, ... K; usually each with 1 year width.
- (2) Tabulate from original data for each interval

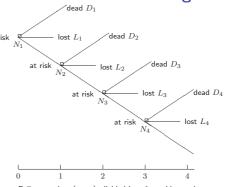
 N_k = size of the **risk set**, *i.e.* the no. of subjects still alive and under follow-up at the start of interval,

 $D_k = \text{ no. of cases}$, *i.e.* deaths observed in the interval,

 $L_k = \text{ no. of losses, i.e. individuals censored during the}$ interval before being observed to die.

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Life table items in a tree diagram



Follow-up time (years), divided into 1-y subintervals

 $N_k = {\sf population}$ at risk at the start of the $k{\sf th}$ subinterval $D_k = \text{no.}$ of deaths, $L_k = \text{no.}$ of losses or censorings in interval k

Life table items for breast ca. patients

(IS: Table 12.2., p. 273, first 4 columns)

| Inter- val | Years since | No. at start of | No. of deaths | No. of losses |
|---------------|----------------|-----------------|---------------|---------------|
| (k) | diagnosis | $\inf_{(N_k)}$ | (D_k) | (L_k) |
| 1 | 0-<1 | 40 | 7 | 0 |
| 2 | 1 - < 2 | 33 | 3 | 6 |
| 3 | 2 - < 3 | 24 | 4 | 3 |
| 4 | 3 - < 4 | 17 | 4 | 4 |
| 5 | 4 - < 5 | 9 | 2 | 3 |
| 6 | 5-<6 | 4 | 1 | 2 |
| 7 | 6-< 7 | 1 | 0 | 1 |
| Total | | | 21 | 19 |

Life table calculations (cont'd)

(3) Calculate and tabulate for each interval

 $N_k' = N_k - L_k/2 = {
m corrected \ size \ of \ the \ risk \ set, \ or}$ "effective denominator" at start of the interval,

 $q_k=D_k/N_k'={
m estimated}$ conditional probability of dying during the interval given survival up to its start,

 $p_k = 1 - q_k = \text{conditional survival proportion over the int'l,}$

 $S_k = p_1 \times \cdots \times p_k =$ cumulative survival proportion from date of diagnosis until the end of the kth interval

= estimate of survival probability up to this time point.

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Follow-up of breast ca. patients (cont'd)

Actuarial life table completed (IS, table 12.2, p. 273)

| Inter- val | Years since dia- gnosis | No. at start of in- terval | No. of deaths | No. of losses | Effec- tive deno- minator | Cond'l prop'n of deaths during int'l | Survival prop'n over int'l | Cumul. survival; est'd survival prob'ty |
|---------------|----------------------------------|--|---------------------|---------------------|------------------------------------|--|-------------------------------------|---|
| (k) | | (N_k) | (D_k) | (L_k) | (N_k') | (q_k) | (p_k) | (S_k) |
| 1 | 0-<1 | 40 | 7 | 0 | 40.0 | 0.175 | 0.825 | 0.825 |
| 2 | 1 - < 2 | 33 | 3 | 6 | 30.0 | 0.100 | 0.900 | 0.743 |
| 3 | 2 - < 3 | 24 | 4 | 3 | 22.5 | 0.178 | 0.822 | 0.610 |
| 4 | 3 - < 4 | 17 | 4 | 4 | 15.0 | 0.267 | 0.733 | 0.447 |
| 5 | 4 - < 5 | 9 | 2 | 3 | 7.5 | 0.267 | 0.733 | 0.328 |
| 6 | 5-< 6 | 4 | 1 | 2 | 3.0 | 0.333 | 0.667 | 0.219 |
| 7 | 6-< 7 | 1 | 0 | 1 | 0.5 | 0.0 | 1.0 | 0.219 |

1-year survival probability is thus estimated 82.5% and 5-year probability 32.8%.

89/ 95

Comparison to previous methods

- ▶ Complement of survival proportion $Q_k = 1 S_k =$ incidence proportion of deaths. Estimates the cumulative risk of death from start of follow-up till end of kth interval
- "Actuarial" indidence rate in the kth interval:

$$I_k = \frac{\text{number of cases } (D_k)}{\text{approximate person-time}}$$

where the person-time is approximated by

$$\left[N_k - \frac{1}{2}(D_k + L_k)\right] \times \text{length of interval}$$

The dead and censored thus contribute half of the interval length.

90 / 95

Survival curve and other measures

Line diagram of survival proportions through interval endpoints provides graphical estimates of interesting parameters of the survival time distribution, *e.g.*:

- ► median and quartiles: time points at which the curve crosses the 50%, 75%, and 25% levels
- ► mean residual lifetime: area under the curve, given that it decreases all the way down to the 0% level.

NB. Often the curve ends at higher level than 0%, in which case some measures cannot be calculated.

Survical curve of breast ca. patients (IS: Fig 12.8)

Numbers above x-axis show the size of population at risk.

92/95

Cause-specific and relative survival

- (A) Cause-specific survival analysis:
 - outcome event: death from the disease C itself,
 - ▶ deaths from other causes → counted as losses.
 - problems with cause of death & competing causes.
- (B) Relative survival analysis: Compute

$$R_k = S_k^{\text{obs}} / S_k^{\text{exp}}$$

the **relative survival proportion** = ratio of

- **observed** survival proportion S_k^{obs} in cancer patients,
- **expected** survival proportion S_k^{exp} based on age-specific mortalities in a reference population (*cf.* SIR!)
- + no information on causes of death needed.

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Ex. Breast cancer patients (cont'd)

Overall and cause-specific (death from breast ca.) survival (**IS**: Fig 12.9 & 12.12, p. 271-3)

Kaplan-Meier curves – alternative to "actuarial":

NB. Meaning of "cause-specific survival"?

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CONCLUSION

Measuring and comparing disease frequencies

- not a trivial task but
- ▶ demands expert skills in epidemiologic methods.

Major challenges:

- obtain the right denominator for each numerator,
- ▶ valid calculation of person-years,
- appropriate treatment of time and its various aspects,
- removal of confounding from comparisons.