

Demography of Diabetes in Denmark

or: How to put real probabilities in your transition matrix and use them

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May 2015

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Demography of diabetes in DK

- ▶ How does diabetes spread in the population?

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- ▶ Life time risk of DM

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- ▶ ... and complications

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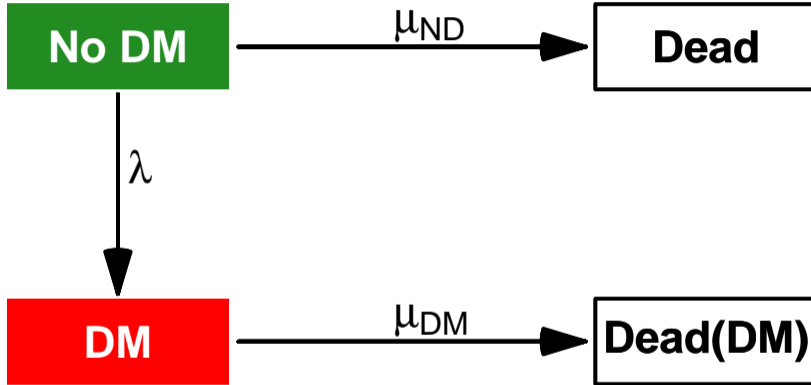
Prevalence of diabetes

- ▶ Prevalence of diabetes has been increasing, while
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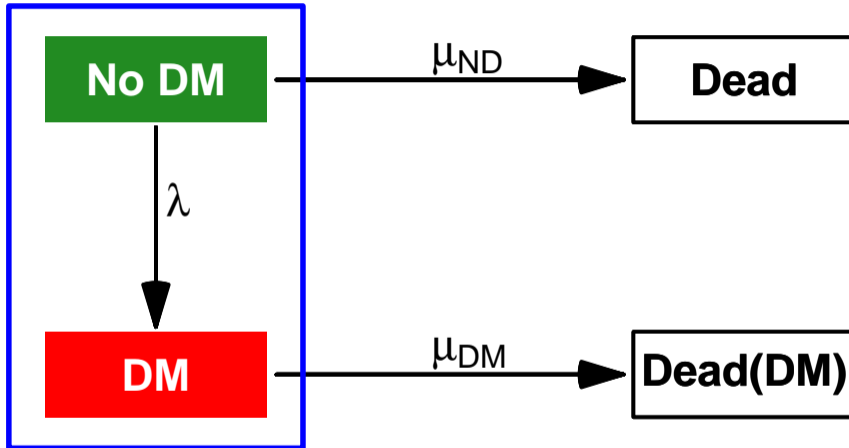
Prevalence of diabetes

- ▶ Prevalence of diabetes has been increasing, while
- ▶ Incidence rates have been **increasing** (4% / year)
- ▶ Mortality rates have been **decreasing** (2% / year)
- ▶ What is the relative contribution of each?

Demographic scenario



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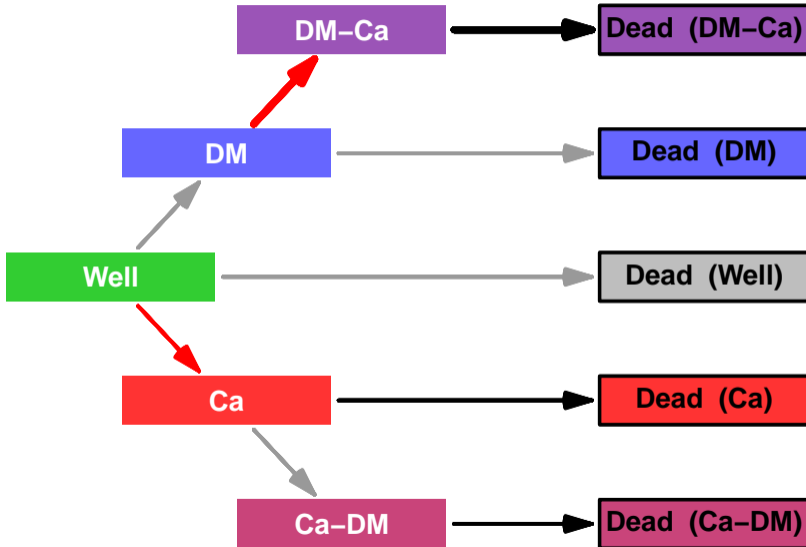
Cancer among diabetes patients

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- ▶ Assess:
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 - ▶ Impact of the DM vs noDM cancer incidence RR

Demographic scenario



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 - ▶ **Age**-specific transition rates
 - ▶ ... as continuous functions of age
 - ▶ ... and possibly other time scales

Prevalence of DM — updating

Transition rates between states as function of a and p :

$$\lambda(a, p), \quad \mu_{\text{ND}}(a, p), \quad \mu_{\text{DM}}(a, p)$$

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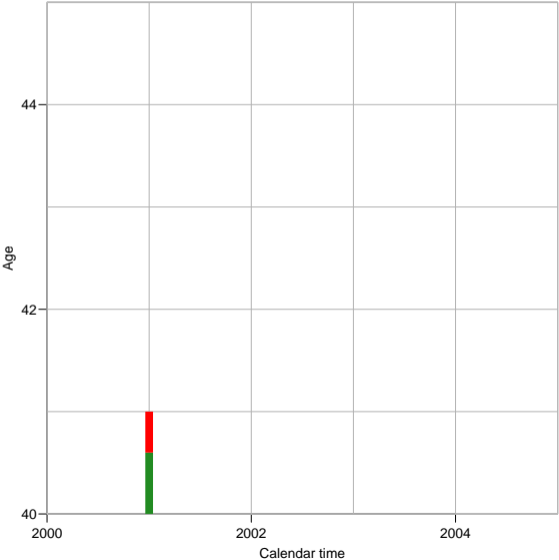
$$P_{\text{ND,ND}}(\ell) = \exp(-(\lambda + \mu_{\text{ND}})\ell)$$

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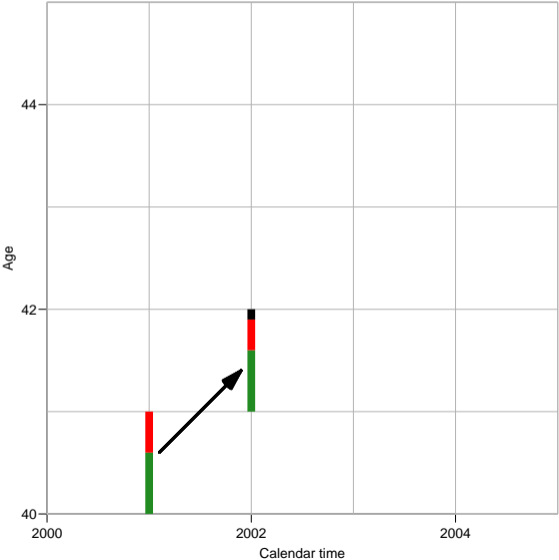
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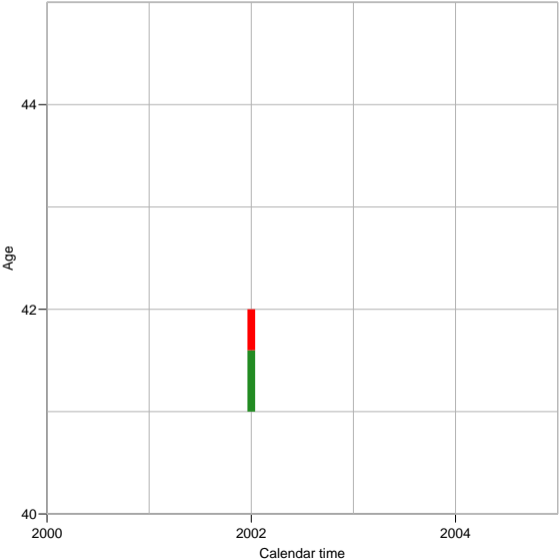
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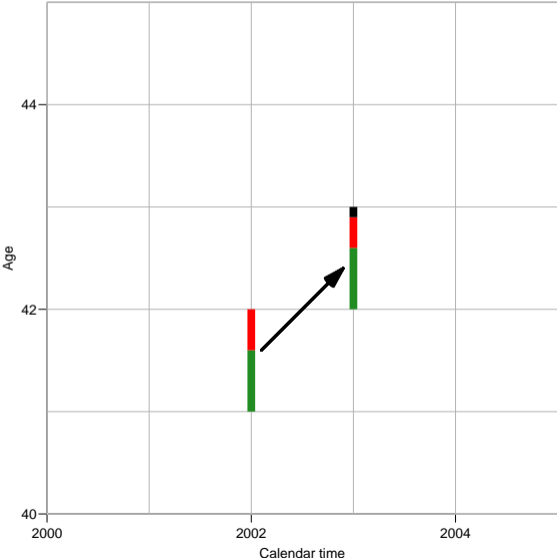
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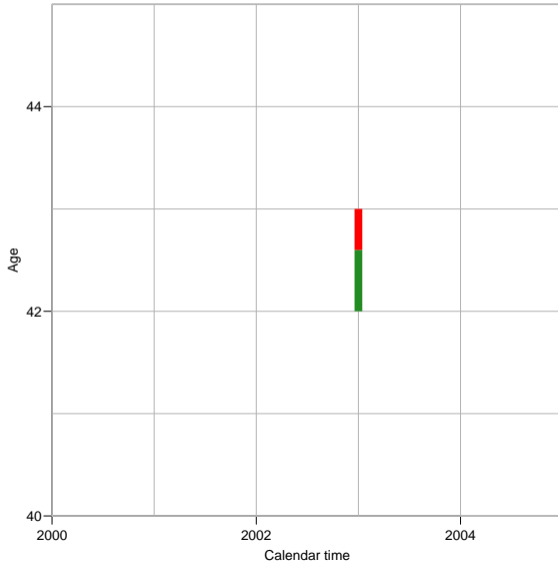
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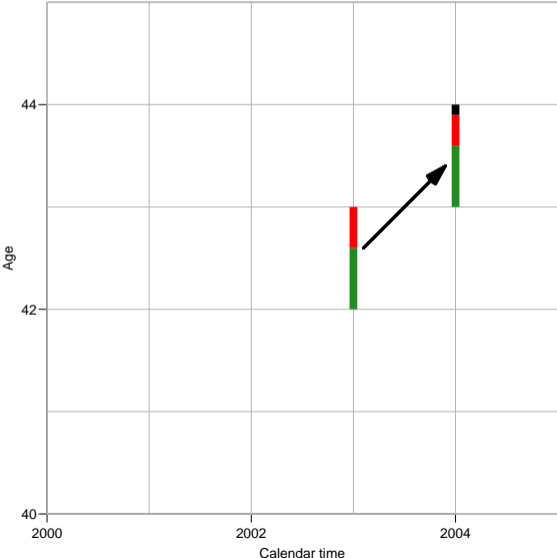
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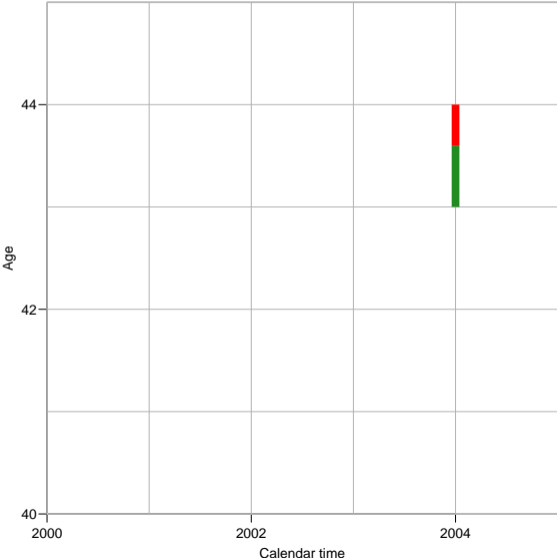
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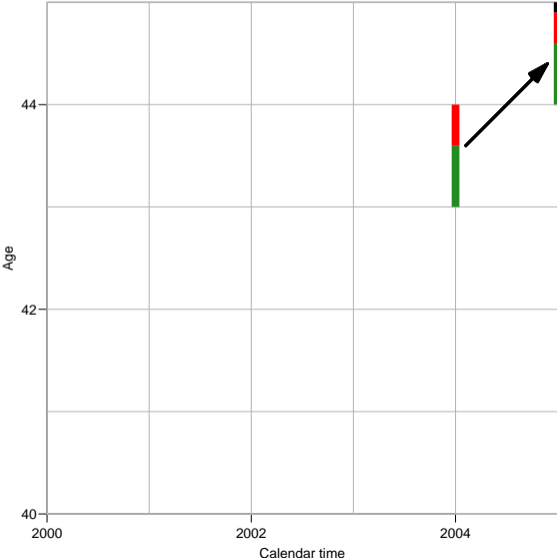
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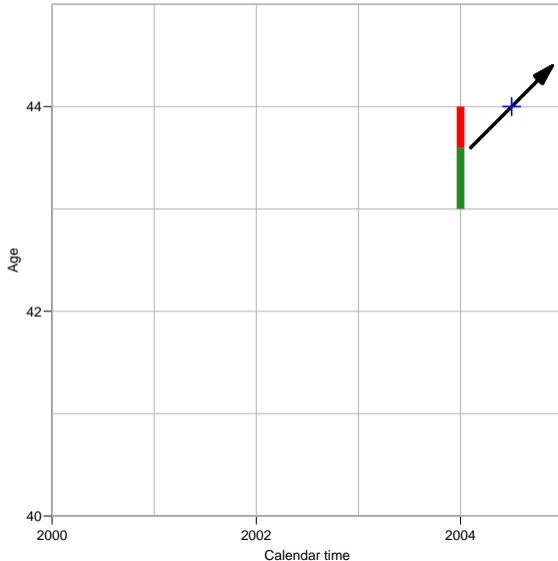
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But where do we get the rates from?

Data base (both studies)

- ▶ National Diabetes Register, 1995–2011

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Incidence and mortality rates: Data

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 - ▶

Incidence and mortality rates: Data

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 - ▶ **Dead**
 - ▶
- ▶ Classification of follow-up (time and events) by age (0–100), calendar time (1995-2011) and date of birth (1-year classes) (Lexis triangles)

Incidence and mortality rates: Data

Example: state **No DM**

- ▶ Time at risk:
 - ▶ **from** date of birth or start of study
 - ▶ **to** date of **DM** or **Dead** or **Ca** (or end of study)
- ▶ Events (transitions)
 - ▶ **DM**
 - ▶ **Dead**
 - ▶ **Ca**
- ▶ Classification of follow-up (time and events) by age (0–100), calendar time (1995-2011) and date of birth (1-year classes) (Lexis triangles)
- ▶ Similarity for the study with cancer states

Incidence and mortality rates: Models

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- ▶ Age-Period-Cohort Poisson-model with smooth effects of A, P & C

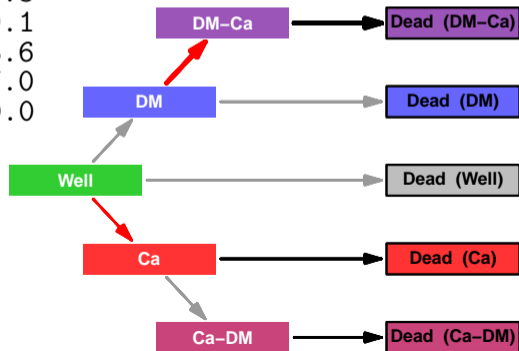
Incidence and mortality rates: Models

- ▶ Incident cases / deaths from each state
- ▶ Person-years in each state
- ▶ Classified by age / date / birth in 1-year classes
- ▶ Age-Period-Cohort Poisson-model with smooth effects of A, P & C
- ▶ Note: Only use the predictions from the models

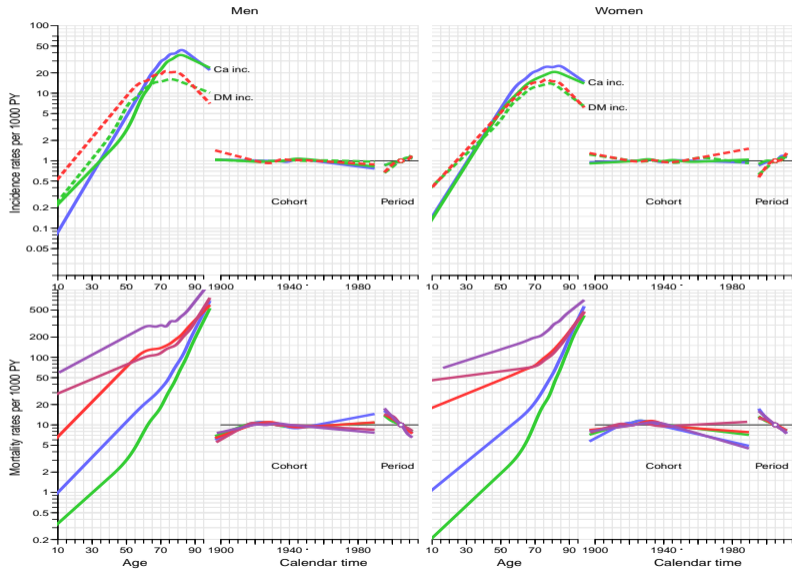
Events and risk time

```
> cbind(  
+ xtabs( cbind( D.ca, D.dm, D.dd ) ~ state, data=dcd ), round(  
+ xtabs( Y/1000 ~ state, data=dcd ), 1 ) )
```

	D.ca	D.dm	D.dd	Y
Well	447419	345400	628705	87502.9
DM	35145	0	73480	2031.3
DM-Ca	0	0	24153	89.1
Ca	0	23508	222966	1973.6
Ca-DM	0	0	14703	117.0
Dead	0	0	0	0.0

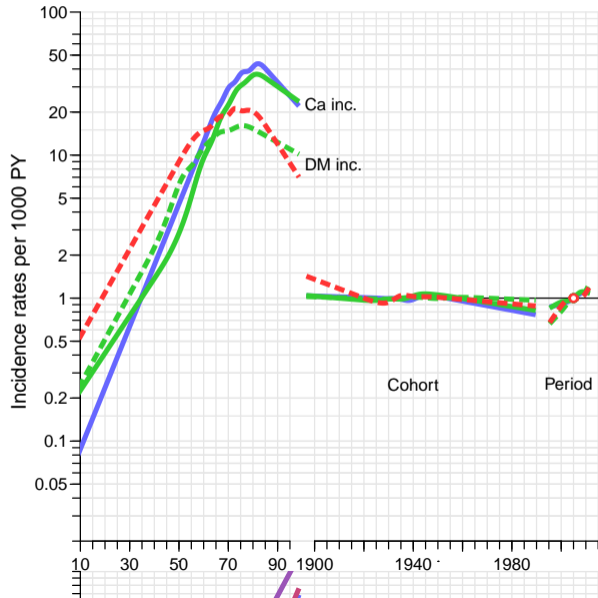


Incidence and mortality rates

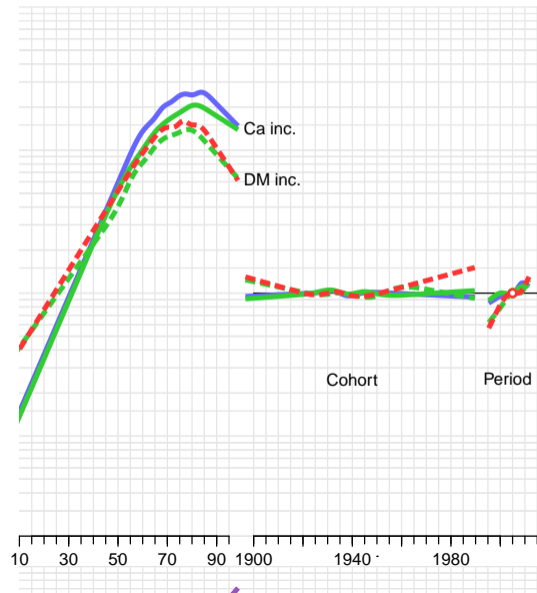


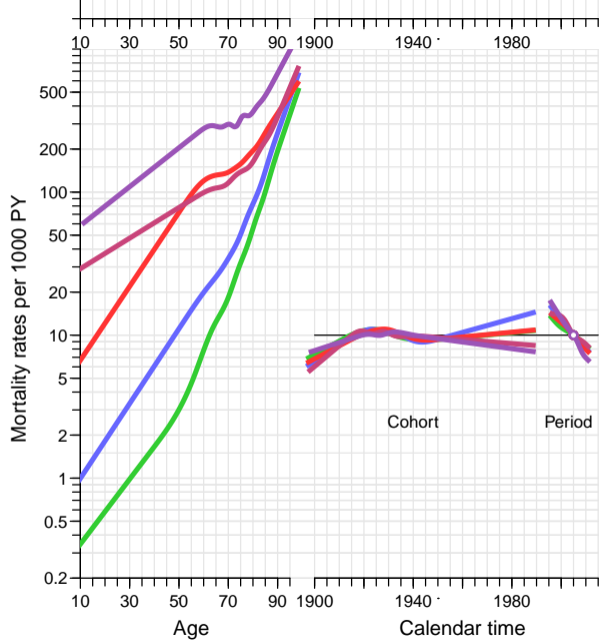
Rate ratio

Men



Women





Transition rates

```
> int <- 1/12
> a.pt <- seq(int,102,int) - int/2

> system.time(
+ for( yy in dimnames(PR)[[4]] )
+ {
+ nd <- data.frame( A=a.pt, P=as.numeric(yy), Y=int )
+
+ PR["Well" , "DM"      , , yy, "M"] <- ci.pred( M.w2dm$model , newdata=nd )[,1]
+ PR["Well" , "Ca"      , , yy, "M"] <- ci.pred( M.w2ca$model , newdata=nd )[,1]
+ PR["Well" , "D-W"     , , yy, "M"] <- ci.pred( M.w2dd$model , newdata=nd )[,1]
+ PR["DM"   , "DM-Ca"   , , yy, "M"] <- ci.pred( M.dm2ca$model , newdata=nd )[,1]
+ PR["DM"   , "D-DM"   , , yy, "M"] <- ci.pred( M.dm2dd$model , newdata=nd )[,1]
+ PR["Ca"   , "Ca-DM"  , , yy, "M"] <- ci.pred( M.ca2dm$model , newdata=nd )[,1]
+ PR["Ca"   , "D-Ca"   , , yy, "M"] <- ci.pred( M.ca2dd$model , newdata=nd )[,1]
+ PR["DM-Ca", "D-DC"   , , yy, "M"] <- ci.pred( M.dc2dd$model , newdata=nd )[,1]
+ PR["Ca-DM", "D-CD"   , , yy, "M"] <- ci.pred( M.cd2dd$model , newdata=nd )[,1]
```

Transition matrices

Use the rates to generate the transition **probabilities**:

```
> print.table( round( addmargins( ci2pr( PR[, , 800, 1, 1] ) * 10^4,  
+                               margin=2 ) ),  
+              zero.print="." )
```

from	to										
	Well	DM	DM-Ca	Ca	Ca-DM	D-W	D-DM	D-Ca	D-DC	D-CD	Sum
Well	9963	8	.	12	.	17	10000
DM	.	9943	16	.	.	.	40	.	.	.	10000
DM-Ca	.	.	9578	422	.	10000
Ca	.	.	.	9815	9	.	.	175	.	.	10000
Ca-DM	9865	135	10000
D-W	10000	10000
D-DM	10000	.	.	.	10000
D-Ca	10000	.	.	10000
D-DC	10000	.	10000
D-CD	10000	10000

State occupancy probabilities

```
> PV <- PR[1,,,,]*0

> for( sc in dimnames(PRp)[["per"]] )
+ for( sx in dimnames(PRp)[["sex"]] )
+   {
+     # Initialize to all well at age 0:
+     PV[,1,sc,sx] <- c(1,rep(0,9))
+     # Compute distribution at endpoint of each age-interval
+     for( ag in 1:dim(PRp)[3] ) PV[,ag,sc,sx] <- PV[ ,max(ag-1,1),sc,sx] %*%
+                                     PRp[, , ag ,sc,sx]
+   }
```

Prediction methods

- ▶ Start all in age 0 in state “**Well**”

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- ▶ Transfer to next possible states in next interval

Prediction methods

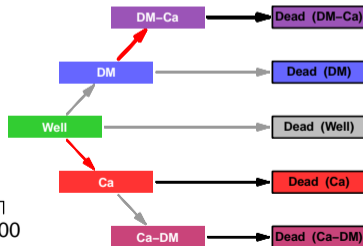
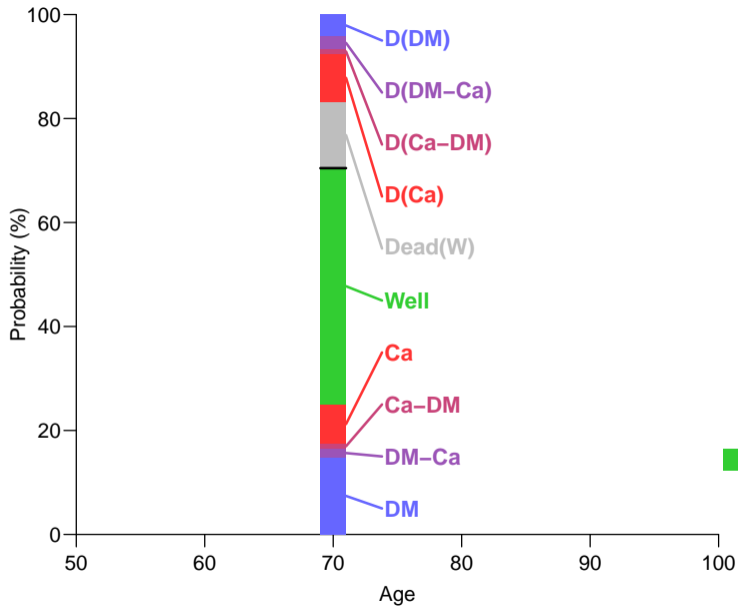
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- ▶ Interval length: 1 month

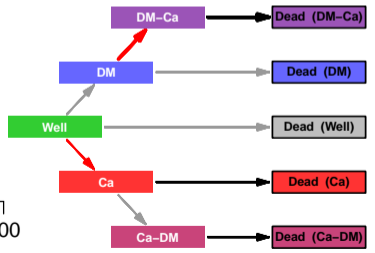
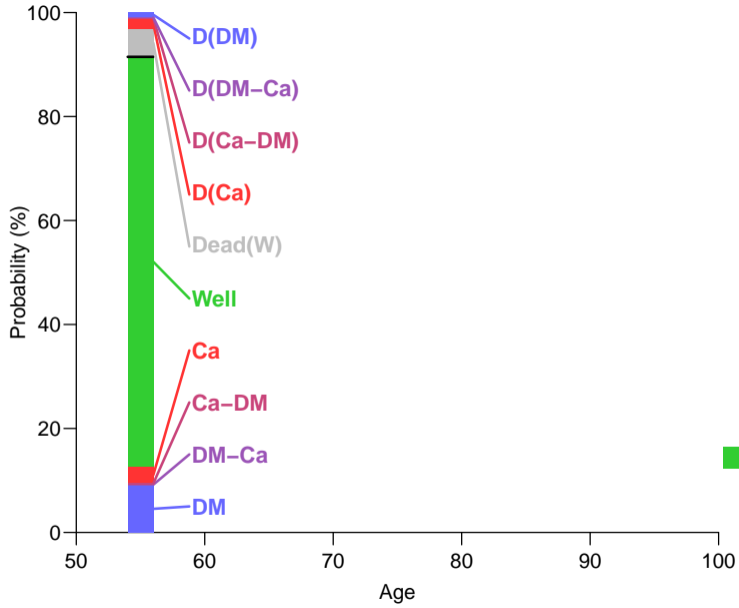
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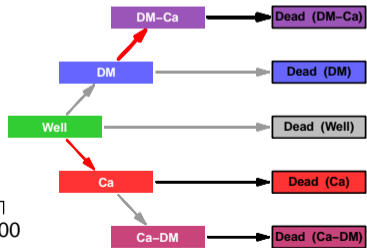
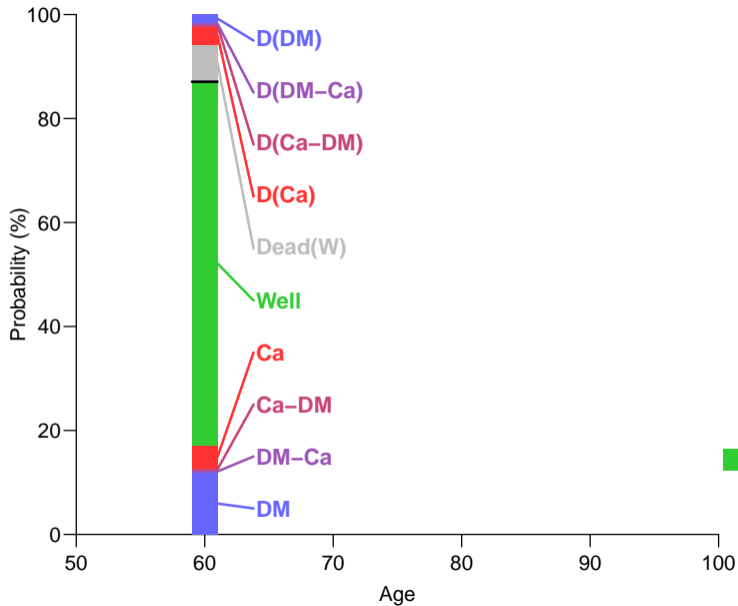
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- ▶ Interval length: 1 month
- ▶ Compute fraction in each state at each age

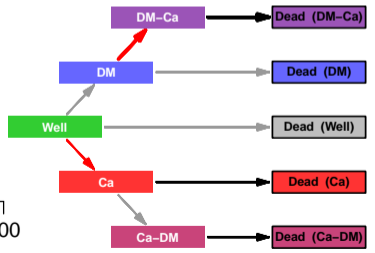
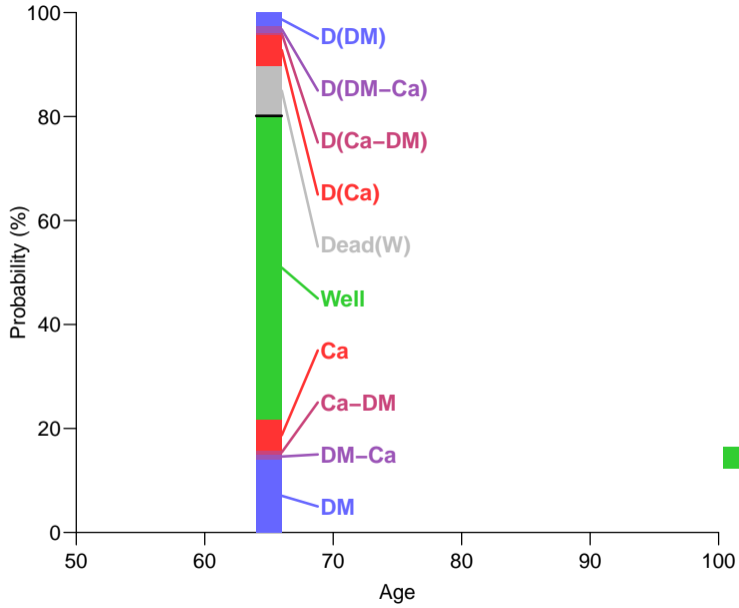
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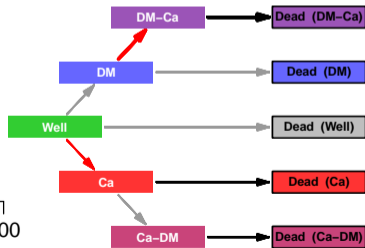
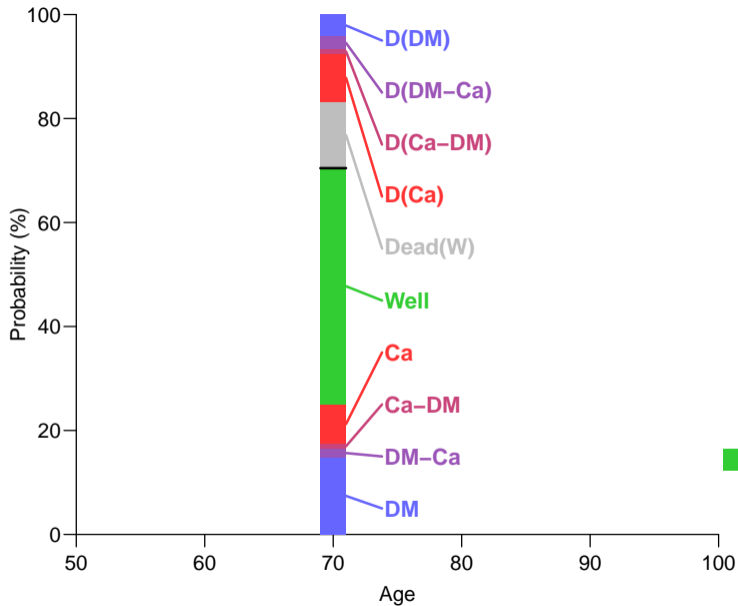
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- ▶ Compute fraction in each state at each age
- ▶ Different scenarios using estimated (cross-sectional) rates at 1 January 1995, 1996, . . . , 2012

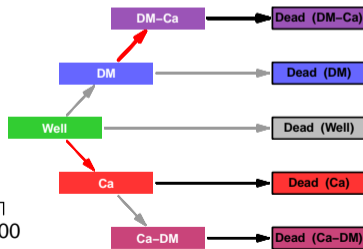
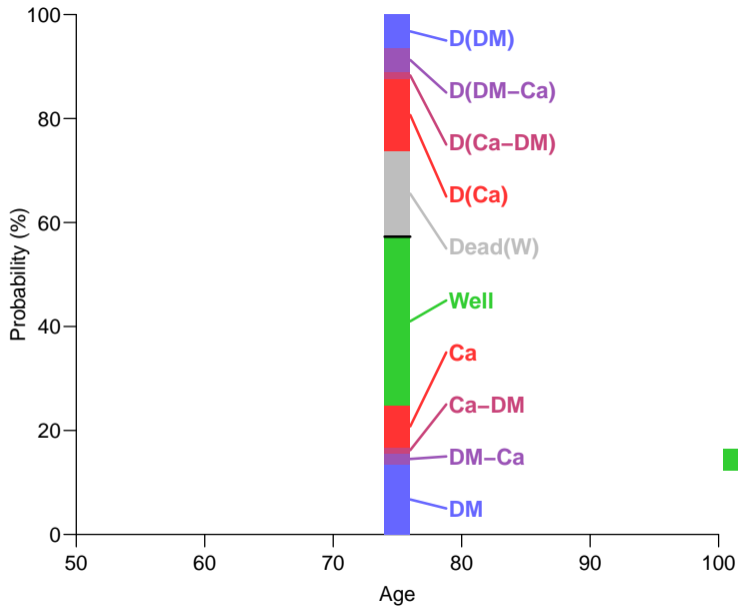


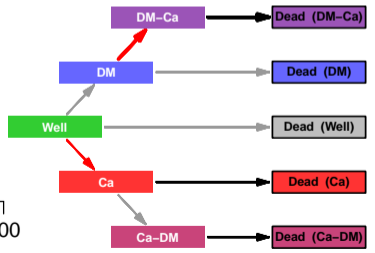
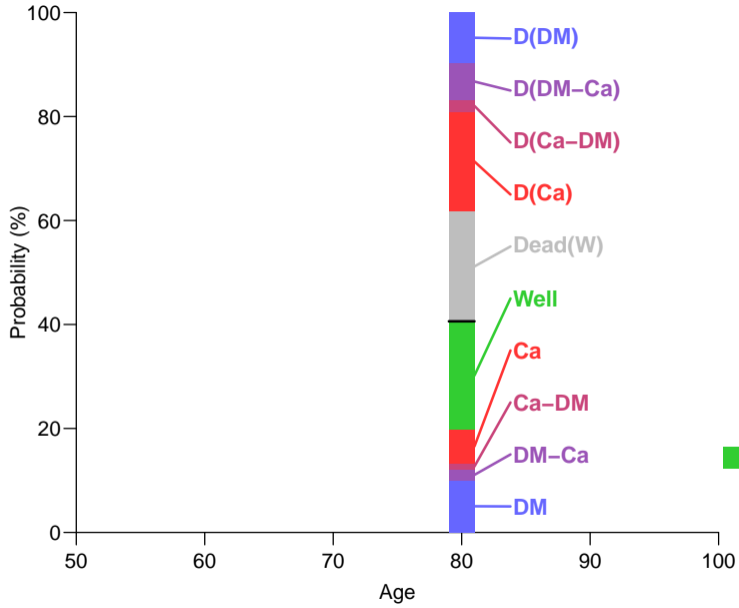


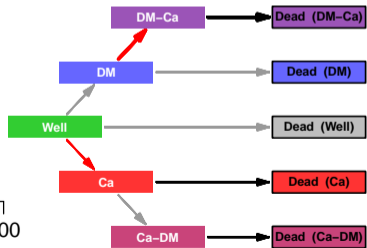
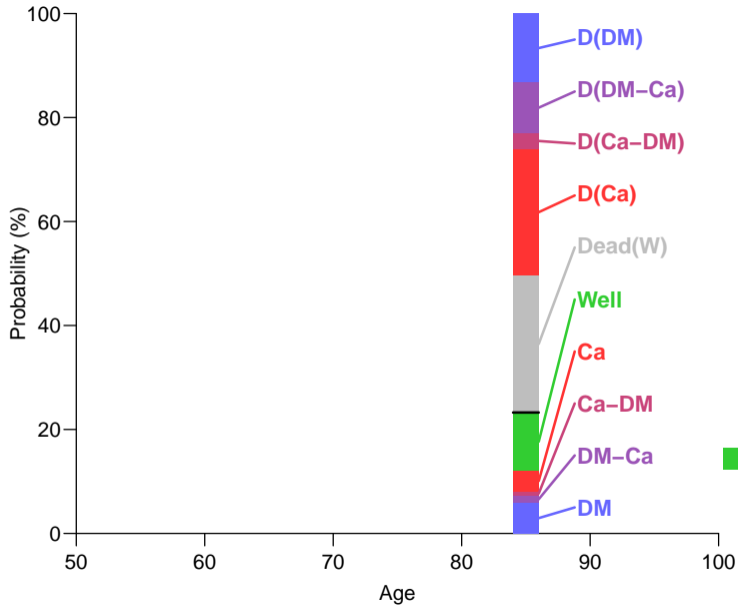


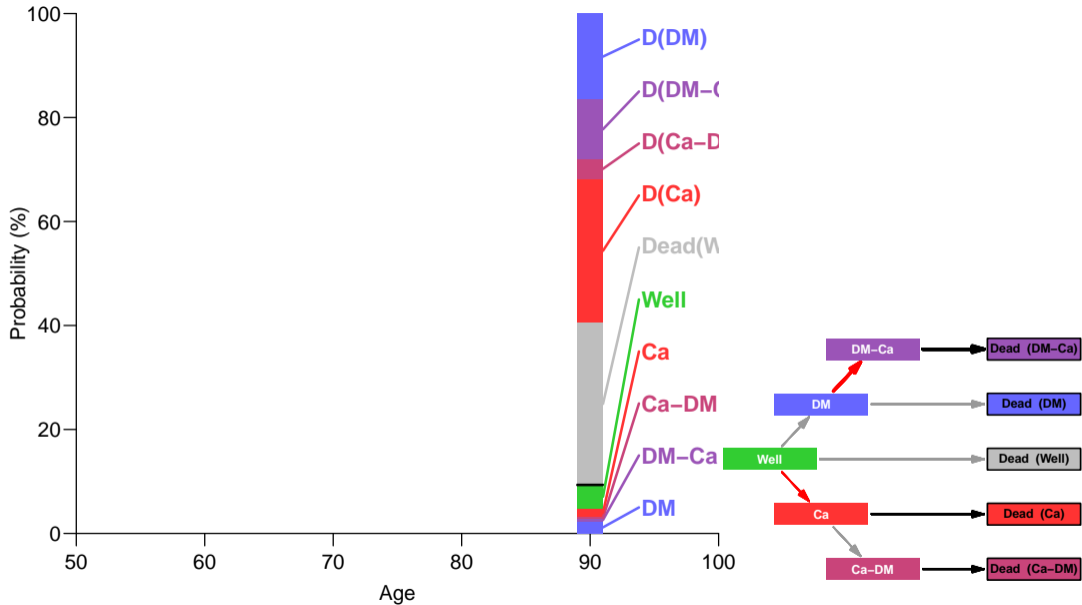


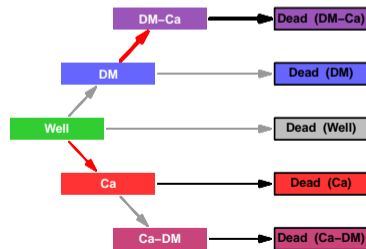
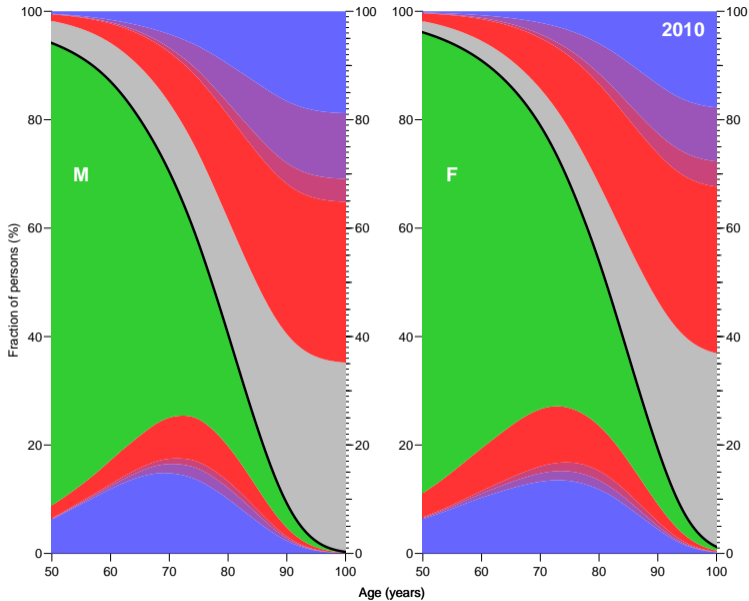


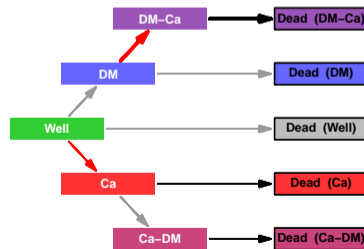
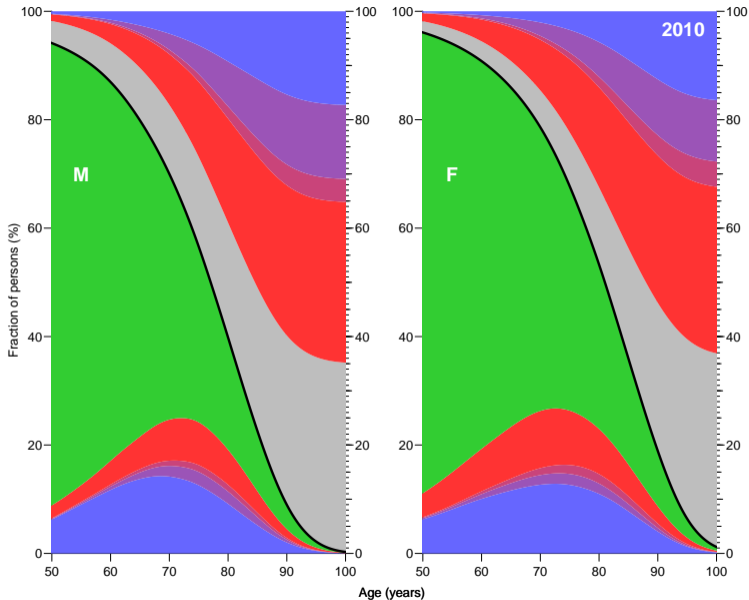




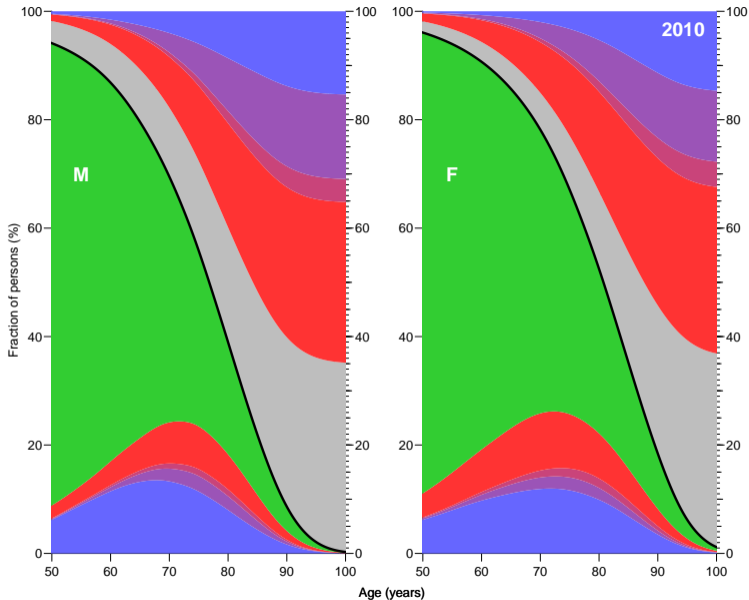






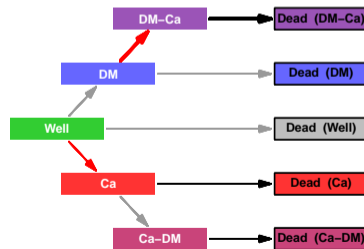


Cancer rates among DM-ptt inflated 20%



Cancer rates among DM-ptt inflated

50%



Transition rates

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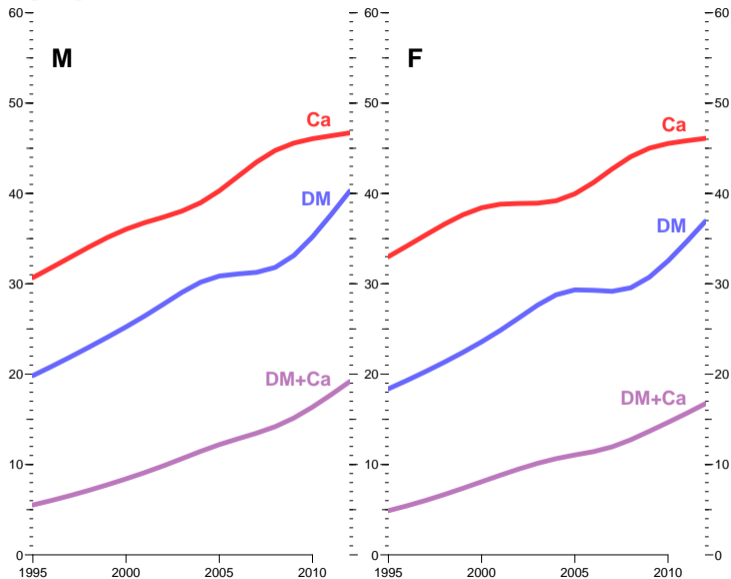
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+ PR["Well" , "DM"      , ,yy, "M"] <- ci.pred( M.w2dm$model , newdata=nd )[,1]
+ PR["Well" , "Ca"      , ,yy, "M"] <- ci.pred( M.w2ca$model , newdata=nd )[,1]
+ PR["Well" , "D-W"     , ,yy, "M"] <- ci.pred( M.w2dd$model , newdata=nd )[,1]
+ PR["DM"   , "DM-Ca"   , ,yy, "M"] <- ci.pred( M.dm2ca$model , newdata=nd )[,1]
+ PR["DM"   , "D-DM"   , ,yy, "M"] <- ci.pred( M.dm2dd$model , newdata=nd )[,1]
+ PR["Ca"   , "Ca-DM"  , ,yy, "M"] <- ci.pred( M.ca2dm$model , newdata=nd )[,1]
+ PR["Ca"   , "D-Ca"   , ,yy, "M"] <- ci.pred( M.ca2dd$model , newdata=nd )[,1]
+ PR["DM-Ca", "D-DC"   , ,yy, "M"] <- ci.pred( M.dc2dd$model , newdata=nd )[,1]
+ PR["Ca-DM", "D-CD"   , ,yy, "M"] <- ci.pred( M.cd2dd$model , newdata=nd )[,1]
```

Transition rates

```
> int <- 1/12
> a.pt <- seq(int,102,int) - int/2

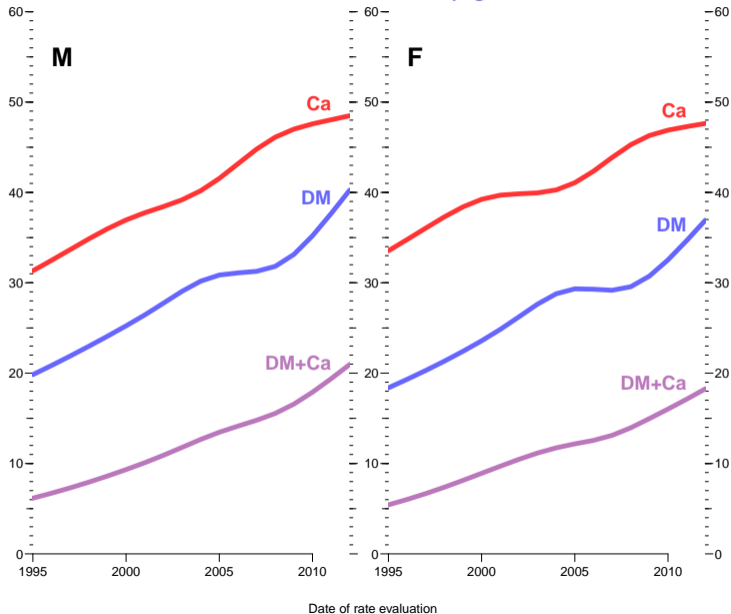
> system.time(
+ for( yy in dimnames(PR)[[4]] )
+ {
+ nd <- data.frame( A=a.pt, P=as.numeric(yy), Y=int )
+
+ PR["Well" , "DM"      , , yy, "M"] <- ci.pred( M.w2dm$model , newdata=nd )[,1]
+ PR["Well" , "Ca"      , , yy, "M"] <- ci.pred( M.w2ca$model , newdata=nd )[,1]
+ PR["Well" , "D-W"     , , yy, "M"] <- ci.pred( M.w2dd$model , newdata=nd )[,1]
+ PR["DM"   , "DM-Ca"   , , yy, "M"] <- ci.pred( M.dm2ca$model, newdata=nd )[,1] * 1.5
+ PR["DM"   , "D-DM"   , , yy, "M"] <- ci.pred( M.dm2dd$model, newdata=nd )[,1]
+ PR["Ca"   , "Ca-DM"  , , yy, "M"] <- ci.pred( M.ca2dm$model, newdata=nd )[,1]
+ PR["Ca"   , "D-Ca"   , , yy, "M"] <- ci.pred( M.ca2dd$model, newdata=nd )[,1]
+ PR["DM-Ca", "D-DC"   , , yy, "M"] <- ci.pred( M.dc2dd$model, newdata=nd )[,1]
+ PR["Ca-DM", "D-CD"   , , yy, "M"] <- ci.pred( M.cd2dd$model, newdata=nd )[,1]
```

Lifetime risks

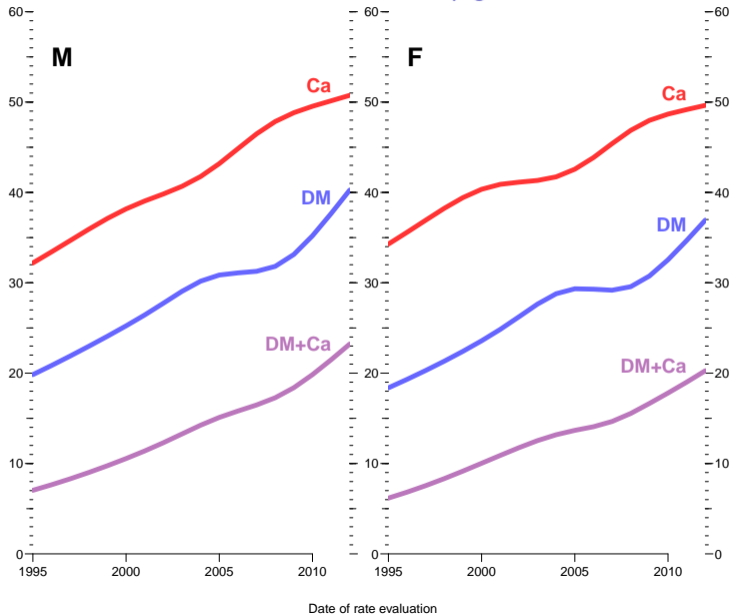


Date of rate evaluation

Lifetime risks - RR inflated 20%



Lifetime risks - RR inflated 50%



Demographic changes in DM & Cancer 1995–2012

- ▶ Changing **rates** in period 1995–2012:

Diabetes incidence	4%/year
Cancer incidence	2%/year
Mortality	-4%/year

Demographic changes in DM & Cancer 1995–2012

- ▶ Changing **rates** in period 1995–2012:

Diabetes incidence	4%/year
Cancer incidence	2%/year
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- ▶ Changing **life-time risk** 1995–2012:

		+20% Ca DM	+50% Ca DM
Diabetes	19% to 38%	19% to 38%	19% to 38%
Cancer	32% to 46%	33% to 48%	34% to 50%
DM + Ca	6% to 18%	6% to 20%	7% to 22%

Conclusion — DM & Cancer

- ▶ Increasing incidence rates of DM and Cancer is what matters for (changes in) lifetime risk...

Conclusion — DM & Cancer

- ▶ Increasing incidence rates of DM and Cancer is what matters for (changes in) lifetime risk. . .
- ▶ **not** the (slightly) elevated risk of Cancer among DM patients.

Prevalence of DM — updating

- ▶ Start with age-specific prevalences 1995

Prevalence of DM — updating

- ▶ Start with age-specific prevalences 1995
- ▶ Use fitted models for incidence and mortality - as function of age and calendar time — to predict prevalences 2012

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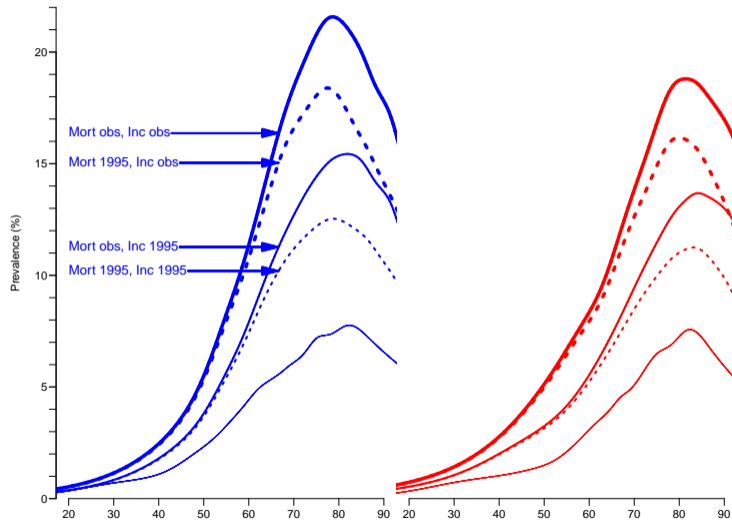
Prevalence of DM — updating

- ▶ Start with age-specific prevalences 1995
- ▶ Use fitted models for incidence and mortality - as function of age and calendar time — to predict prevalences 2012
- ▶ Assume:
 - ▶ Incidence rates had remained at 1995 level
 - ▶ Mortality rates had remained at 1995 level
 - ▶ Both had remained at 1995 level

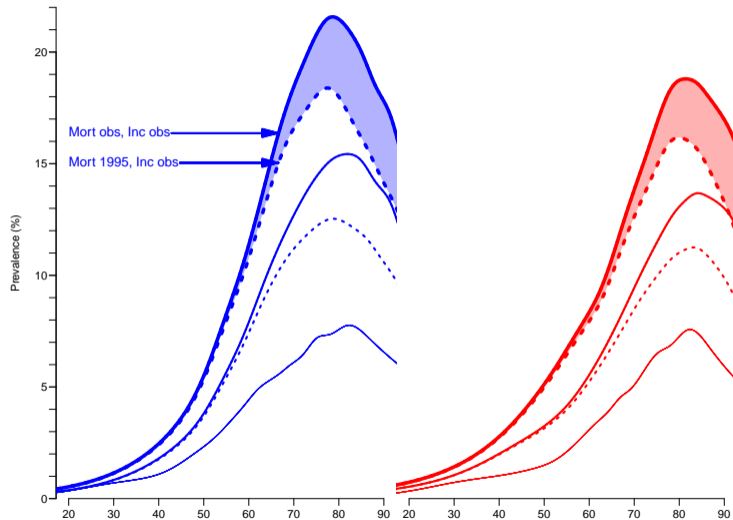
Prevalence of DM — updating

- ▶ Start with age-specific prevalences 1995
- ▶ Use fitted models for incidence and mortality - as function of age and calendar time — to predict prevalences 2012
- ▶ Assume:
 - ▶ Incidence rates had remained at 1995 level
 - ▶ Mortality rates had remained at 1995 level
 - ▶ Both had remained at 1995 level
- ▶ Differences between predicted prevalences gives the contribution from incidence rate changes, mortality rate changes and 1995 disequilibrium.

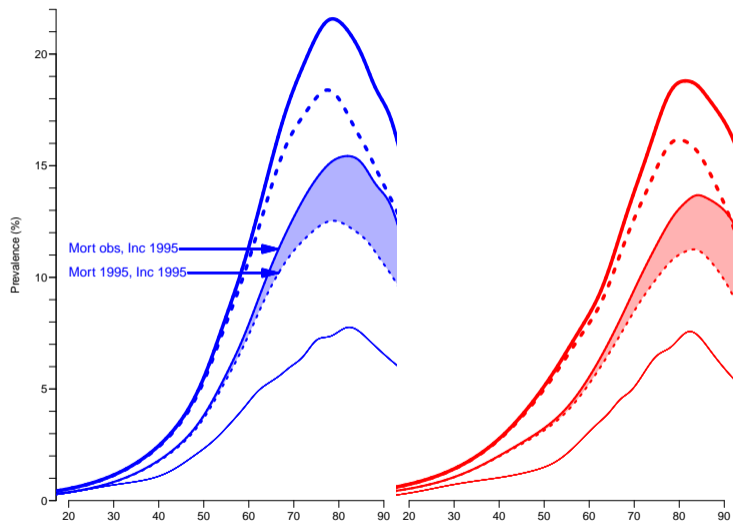
Prevalence of DM — updating



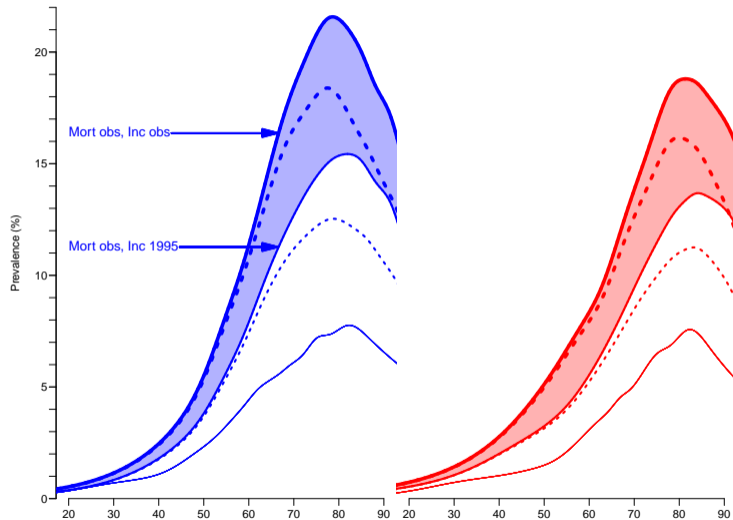
Prevalence of DM — updating



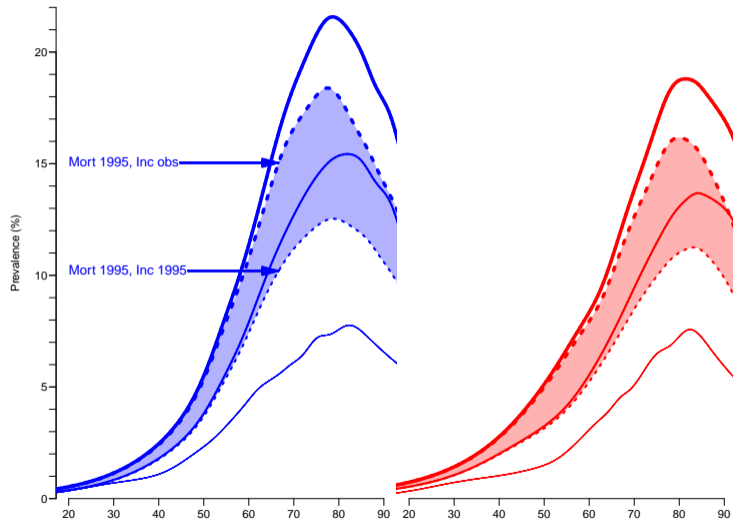
Prevalence of DM — updating



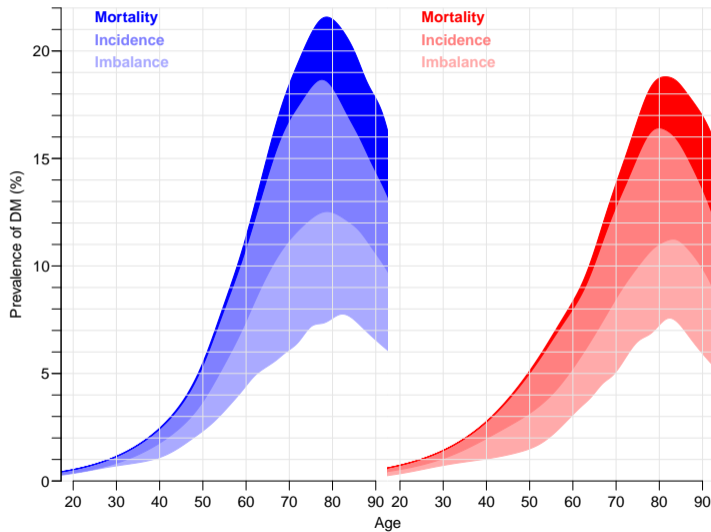
Prevalence of DM — updating



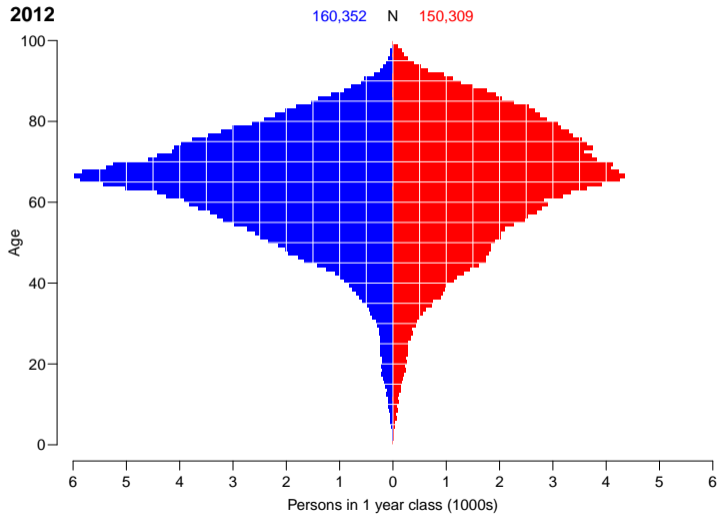
Prevalence of DM — updating



Components of prevalent cases

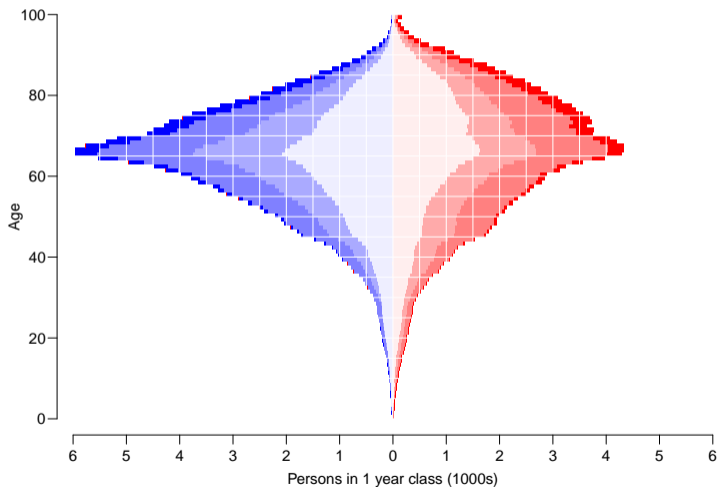


Prevalent cases



Components of prevalent cases

2012	Mort	Inc	Imbal	Org	All	N	All	Org	Imbal	Inc	Mort
	12,273	47,282	40,568	61,510	161,632		152,001	55,939	38,232	46,486	11,344
	7.6	29.3	25.1	38.1		%		36.8	25.2	30.6	7.5



Thanks for your attention

